

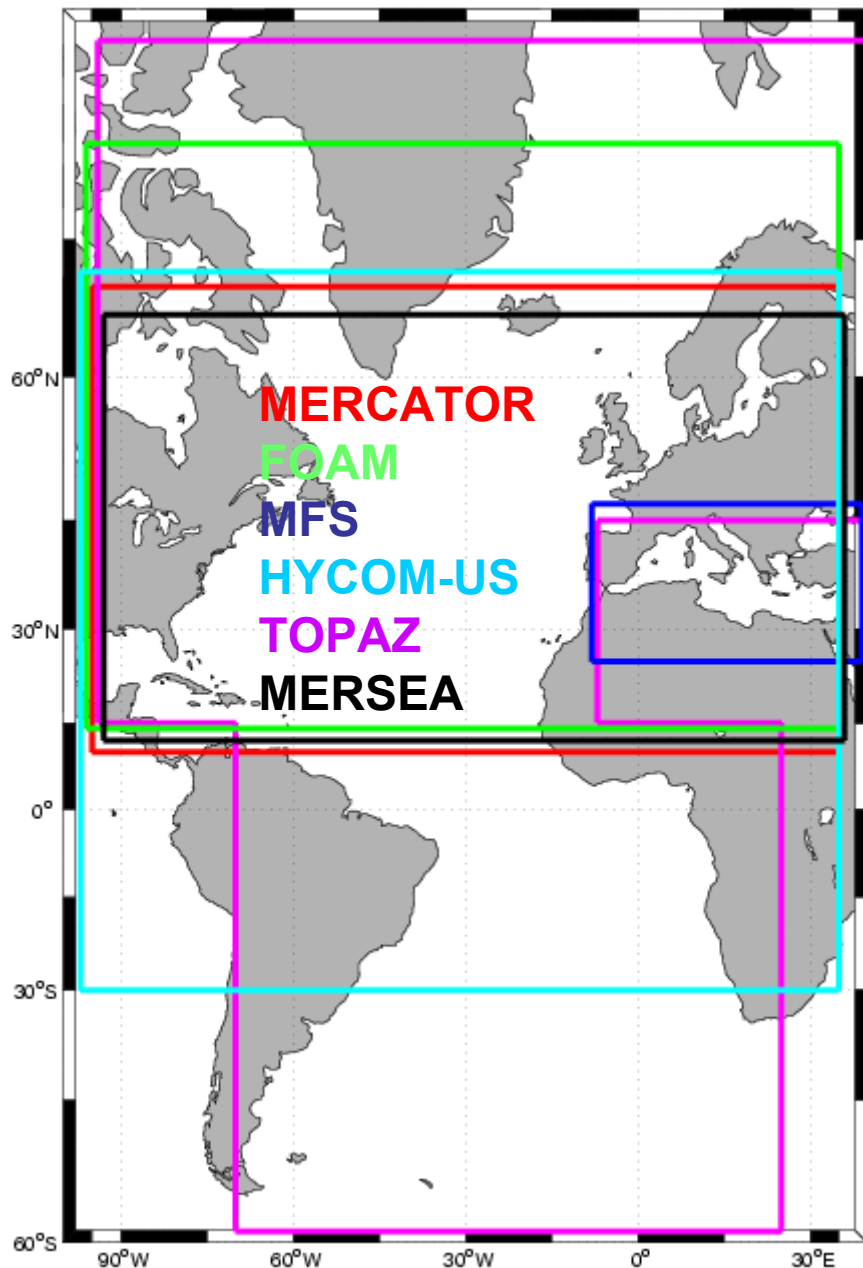
# MERSEA Strand1

## Atlantic and Mediterranean Sea prototype Project: An Inter-comparison of 5 Forecasting Systems

**Laurence Crosnier , Christian Le Provost and Mersea Team**

**GOAL=GMES +GODAE:** Evaluate the strength/weakness of  
[4 European + 1 US] Ocean monitoring and forecasting systems.

[www.mersea.eu.org](http://www.mersea.eu.org)



**MERSEA-STRAND1 2003-2004**

<b>MERCATOR FR</b>	OPA -Z coord./Rigid Lid	-horiz. 1/15° (5-7km) 43 levels  -Atl+Med from 10 to 70°N.
<b>FOAM UK</b>	HADLEY CENTRE -Z coord./Rigid Lid	-horiz. 1/9° (12km) 20 levels  -Atl+Med from 10 to 70°N.
<b>MFS IT</b>	MOM 1.1 -Z coord./Rigid Lid	-horiz. 1/8° 31 levels  - Med only
<b>HYCOM US</b>	HYCOM 2.1 -Hybrid coord./Free surface	-Horiz 1/12° (6.5km) 26 hybrid layers  -Atl+Med from 28°S to 70°N, 98°W to 36°W.
<b>TOPAZ NO</b>	HYCOM -Hybrid coord/Free surface	-horiz. 20 to 30km 22 hybrid layers  -Arctic+Atlantic till 60°S. No med basin.

<b>MERCATOR FR</b>	<b>OPA</b> <b>-Z coord./Rigid Lid</b>  -Simple thermo. ice model <b>-SPIN UP 15days</b> -TKE	<b>-horiz. 1/15° (5-7km)</b> <b>43 levels</b> -Atl+Med from 10 to 70°N. -Relaxation to Medatlas (T,S) in Gulf of Cadiz below 500m	<b>-Daily ECMWF forcing</b>  -Relaxation to Reynolds SST and Reynaud SSS -Monthly river runoff -Data assimilation stopped at depth 500m	<b>-OI SOFA</b> <b>-SLA along track</b> (Jason1,ERS2/Envisat,GFO) once a week  -MSSH from Rio et al.(data) in the Atlantic and blend of previous runs in MED	<b>ATL</b> <b>MED</b>
<b>TOPAZ NO</b>	<b>HYCOM</b> <b>-Hybrid coord/Free surface</b>  -dyn./thermodynamic sea ice <b>-SPIN UP 20years</b> -KPP mixing	<b>-horiz. 20 to 30km</b> <b>22 hybrid layers</b>  -Artic+Atlantic till 40°S. Closed boundary without relaxation. No med basin.	<b>-6 hourly ECMWF forcing (Bulk formulae momentum&amp;heat)</b>  -Precip Clim+ Relaxation to Levitus SSS(60days) -No river runoff -Data assimilation stopped at depth 300m	<b>-EnKF</b>  <b>-SLA Maps(SALTO-DUACS)</b> once a week <b>-SST</b> from CLS AVHRR data once a week <b>-Maps of ice concentration</b>  -MSSH from OCCAM run	<b>ATL</b>
<b>FOAM UK</b>	<b>HADLEY CENTRE</b> <b>-Z coord./Rigid Lid</b>  -dyn./thermodynamic sea ice <b>-SPIN UP 5months</b> -Kraus-Turner	<b>-horiz. 1/9° (12km)</b> <b>20 levels</b>  -Atl+Med from 10 to 70°N.	<b>-6 Hourly NWP-MetOffice forcing</b>  -Weak relaxation to Levitus SST and SSS. -No river runoff -Data assimilation stopped at depth 300m	<b>-OI Cooper&amp;Haines</b> <b>-SLA along track</b> (Jason1,GFO;Envisat) <b>-SST 2.5° gridded</b> (ARGO)Once a day. <b>-T+S profiles</b> at all depths <b>-gridded ice concentration</b> -MSSH from previous run	<b>ATL</b> <b>MED</b>
<b>MFS IT</b>	<b>MOM 1.1</b> <b>-Z coord./Rigid Lid</b>  -no ice model <b>-SPIN UP:7years</b> -cst vertical mixing+vertical adjustment	<b>-horiz. 1/8°</b> <b>31 levels</b>  - Med only -Transport through Gibraltar parameterized	<b>-6 Hourly ECMWF forcing (Bulk formulae momentum &amp; heat)</b>  -relaxation to satellite night time SST and SSS climato -No river runoff -Data assimilation stopped at depth 1000m	<b>-OI SOFA</b>  <b>-SLA along track</b> (SALTO-DUACS) once a week <b>-SST+T profiles</b> along track once a week  -MSSH from previous run with 1993-99 forcing.	<b>MED</b>
<b>HYCOM US</b>	<b>HYCOM 2.1</b> <b>-Hybrid coord/Free surface</b>  -no ice model <b>-SPIN UP 15years</b> -KPP mixing	<b>-Horiz 1/12° (6.5km)</b> <b>26 hybrid layers</b>  -Atl+Med from 28°S to 70°N, 98°W to 36°W. -Entrainment param. of Med Water outflow	<b>-3 hourly NOGAPS forcing (Bulk formulae for heat)</b> -SSS= 50%(E-P) +50% relaxation to Levitus SSS -relaxation to MODAS SST ana. -monthly river runoff -Data assimilation stopped at	<b>-OI Cooper&amp;Haines</b>  <b>-SLA MODAS Maps</b> (Jason1 GFO ERS2)  -MSSH from 1/12° MICOM (ECMWF)	<b>ATL</b>

## **Metrics** have been defined for the **North Atlantic** and the **Mediterranean Sea**

- **Fields provided** : Daily mean Best Estimate + (T0+6) forecast.
- **1YEAR Time period** : JUNE 2003-JUNE 2004.
- **2 BASINS** : Atlantic + Mediterranean Sea
- **CLASS1** T, S, U, V, SSH, MLD, BSF, Tx, Ty, Qtot+relax., E-P-R +relax., MSSH

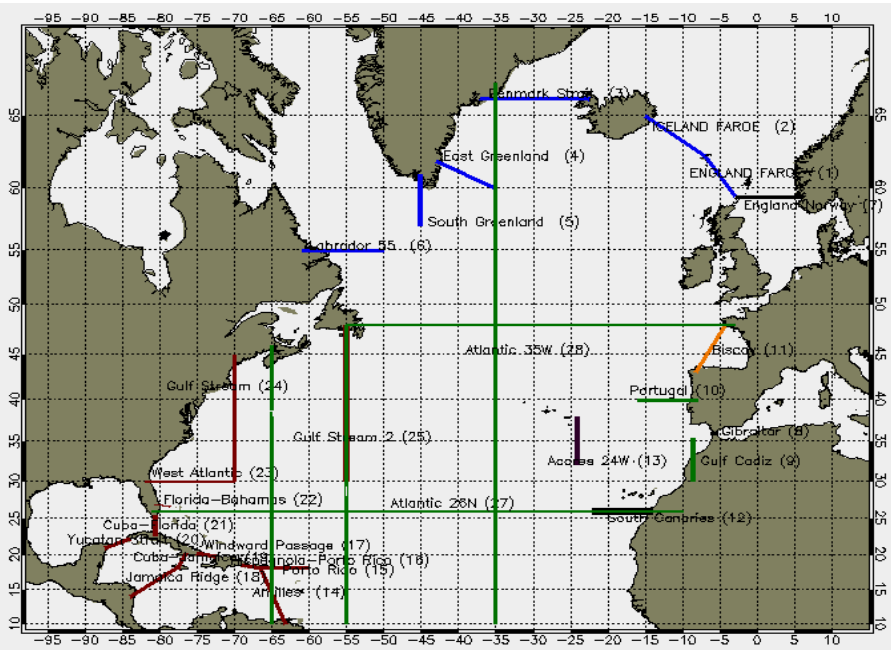
### **Interpolation on 1/8° horizontal grid**

with 12 vert. levels in ATL (5;30;50;100;200;400;700;1000;1500;2000;2500;3000m)

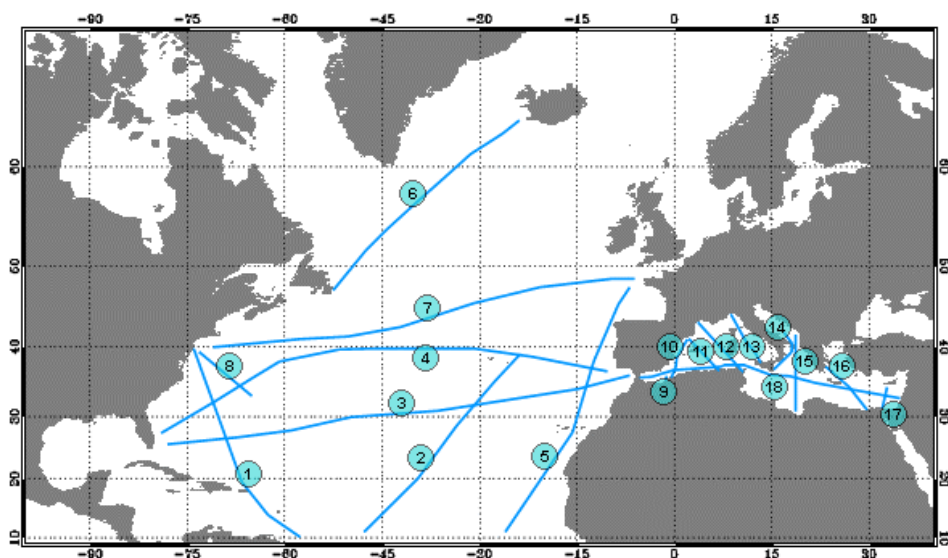
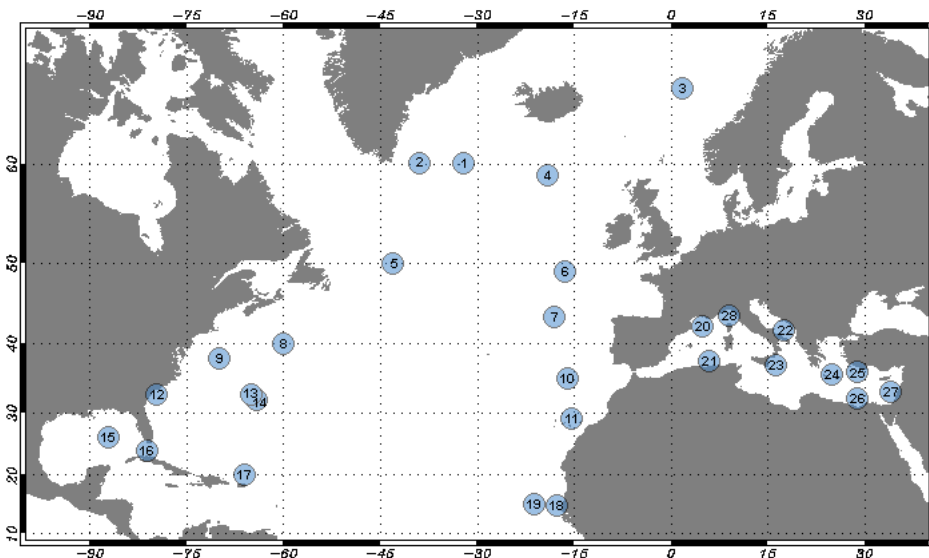
8 vert. levels in MED (5;30;50;100;200;500;1000;2000m).

- **CLASS2** High resolution (T,S,U,V) sections/moorings.
- **CLASS3** Daily mean volume transports through sections  
Meridional Heat Transport  
Overturning Stream Function  $/z/\sigma/\theta$
- **CLASS4** Test performance of analysis and forecasts.
- **Available : CLASS1 + CLASS2 + CLASS3**
- **working on CLASS4**

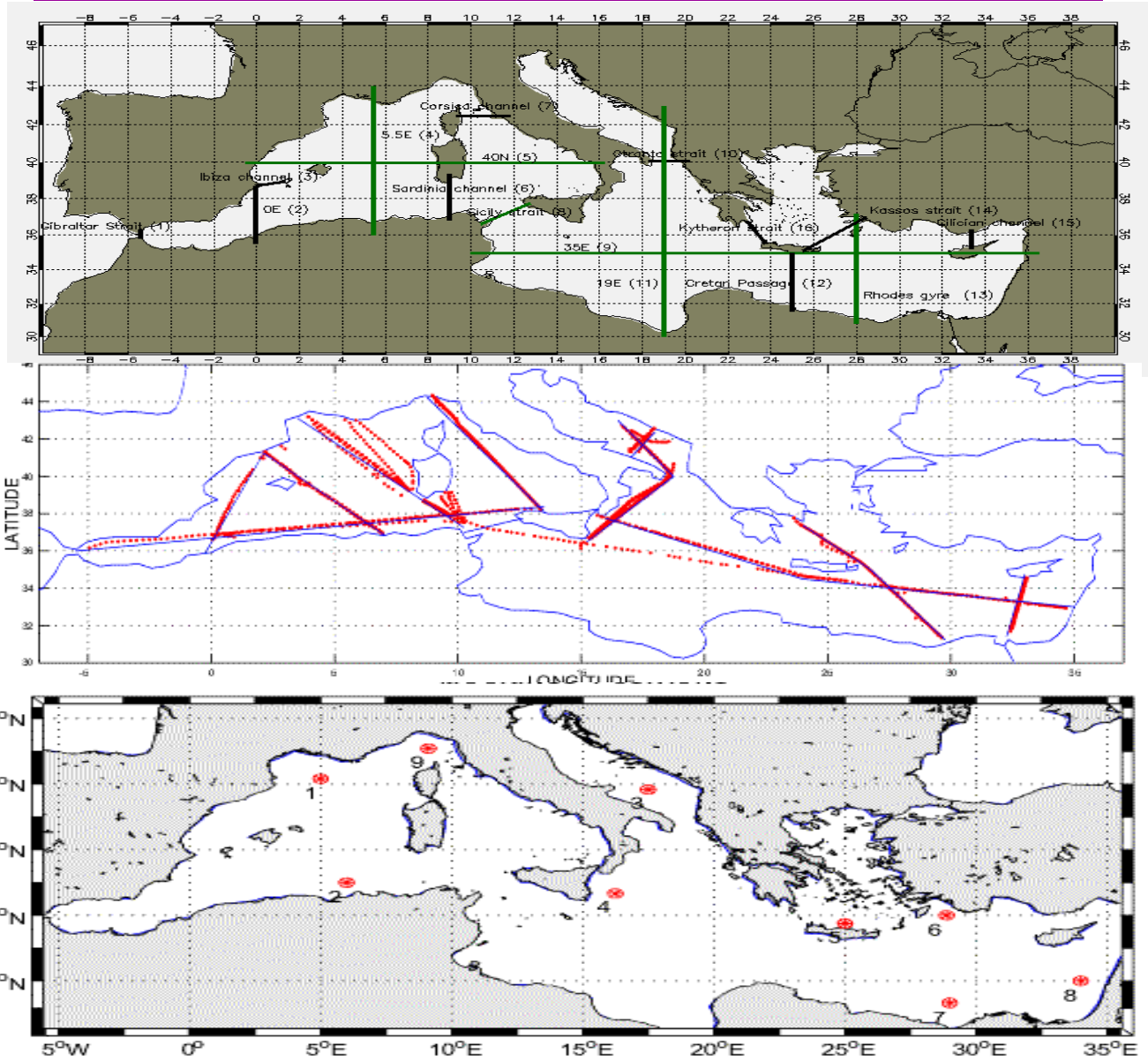
# CLASS 2 in the Atlantic



Mouillages MERSEA



# CLASS 2 In the Mediterranean Sea



# STRATEGY BASED ON FOLLOWING TECHNOLOGY

- **Common GRID + Netcdf FORMAT**
- **DATA STORED ON OPENDAP SERVERS**

<http://user:password@opendap.mercator-ocean.fr/dodsC/>

<http://thredds.sincem.unibo.it:8080/thredds/dodsC/>

<http://user:password@www.nerc-essc.ac.uk:9090/dodsC/>

<http://mersea.nerc.no/dodsC/>

<http://hycom.rsmas.miami.edu/dodsC/>

- **DODS/MATLAB or DODS/IDL or DODS/Ferret**

```
>> loaddods('http://www.nerc-essc.ac.uk:9090/FOAM_NAT?temperature[0][0]')
```

Reading: [http://www.nerc-essc.ac.uk:9090/FOAM\\_NATL\\_120\\_8th\\_ARC](http://www.nerc-essc.ac.uk:9090/FOAM_NATL_120_8th_ARC)

Constraint: temperature[0][0]

Server version: catalogaggserver/0.8

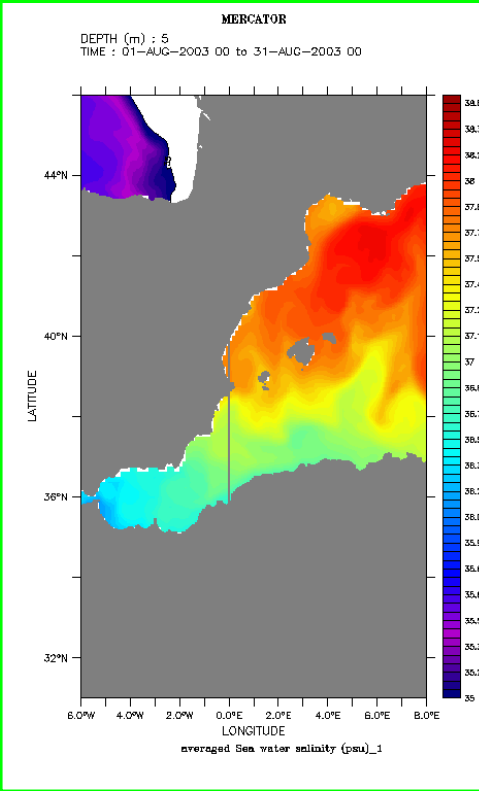
Creating matrix temperature (1 x 1 x 441 x 869) with 383229 elements.

Creating vector time with 1 elements.

Creating vector depth with 1 elements.

Creating vector latitude with 441 elements.

Creating vector longitude with 869 elements.



Live Access to Data - Microsoft Internet Explorer

Adresse http://las.mercator-ocean.fr/las/servlets/analysis

MERCATOR Live Access Server

Search dataset/variable:  Go

single data set compare two

Datasets > MERCATOR > MEDITERRANEAN > Mercator long term best estimate time serie

Variable(s): Sea water salinity (psu)

Create a new variable based on the the available analyses. Choose the axes and regions to apply and then click on **Next >** Help

Select analysis type: **Average** *Other choices: min/max, average, variance* Next > Cancel >

Name for this variable: Sea water salinity

Apply to these axes:  X  Y  Z  T  T

Mask: None  Ocean  Land

Select range for applicable axis: *Don't use map applet*

Latitude: 46.0 N, 30.0 N  
Longitude: 6.0 W, 36.5 E  
Zoom In Zoom Out

Z range: 5 to 5  
2000 to 2000

T range: **01-Aug-2003** to **01-Aug-2003**  
**31-Aug-2003** to **31-Aug-2003**

Contact us, Subscribe, Search, Site map, Home, Project group, Scientific aspects

Live Access to Data - Microsoft Internet Explorer

Adresse http://las.mercator-ocean.fr/las/servlets/data

MERCATOR Live Access Server

single data set compare two

Datasets > MERCATOR > MEDITERRANEAN > Mercator long term best estimate time serie

Variable(s): Sea water salinity averaged (psu)\_1 (from Sea water salinity (psu))

You may modify the appearance of the plot. The navigation bar on the left will be updated.

Output

DEPTH (m) : 5  
TIME : 01-AUG-2003 00 to 31-AUG-2003 00

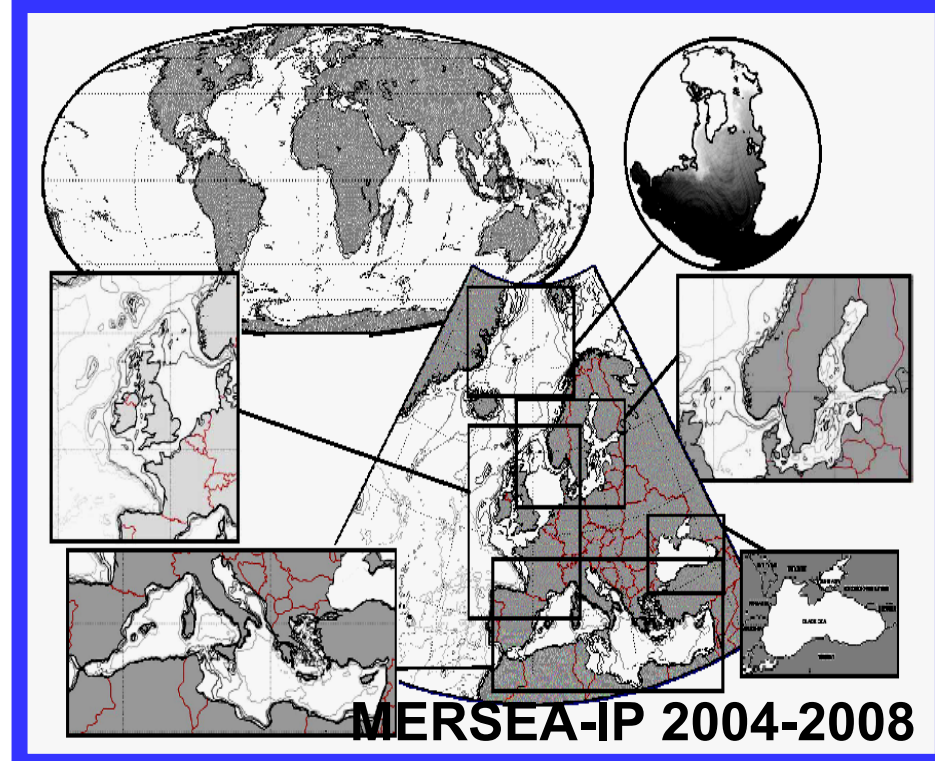
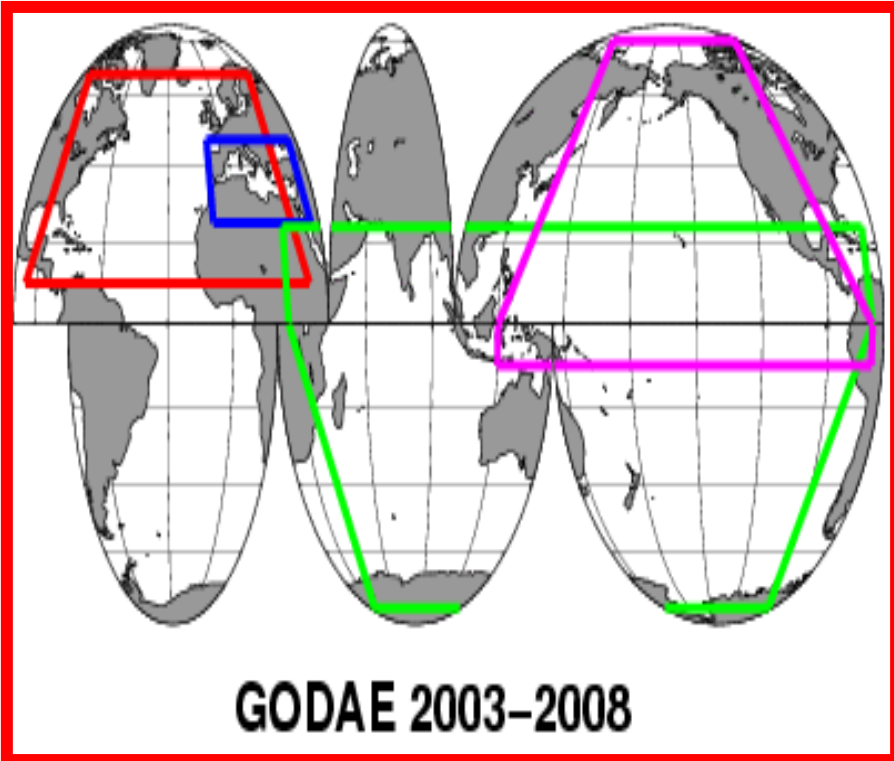
Latitude: 46°N, 42°N, 38°N, 34°N, 30°N  
Longitude: 0°E, 10°E, 20°E, 30°E

Sea water salinity averaged (psu)\_1

Send all plot output to new window

LAS USE EXAMPLE  
<http://las.mersea.eu.org>





**GLOBAL (France, US)**  
**North ATLANTIC + Mediterranean**  
**SEA (Mersea systems)**  
**INDIAN , SouthPACIFIC,**  
**AUSTRAL Ocean**  
**(Blue Link, Australia)**  
**North PACIFIC (Japan)**

**North ATLANTIC**  
**Baltic**  
**Arctic**  
**Mediterranean Sea**  
**(16 countries, 40 organizations)**

# Inter-Comparison

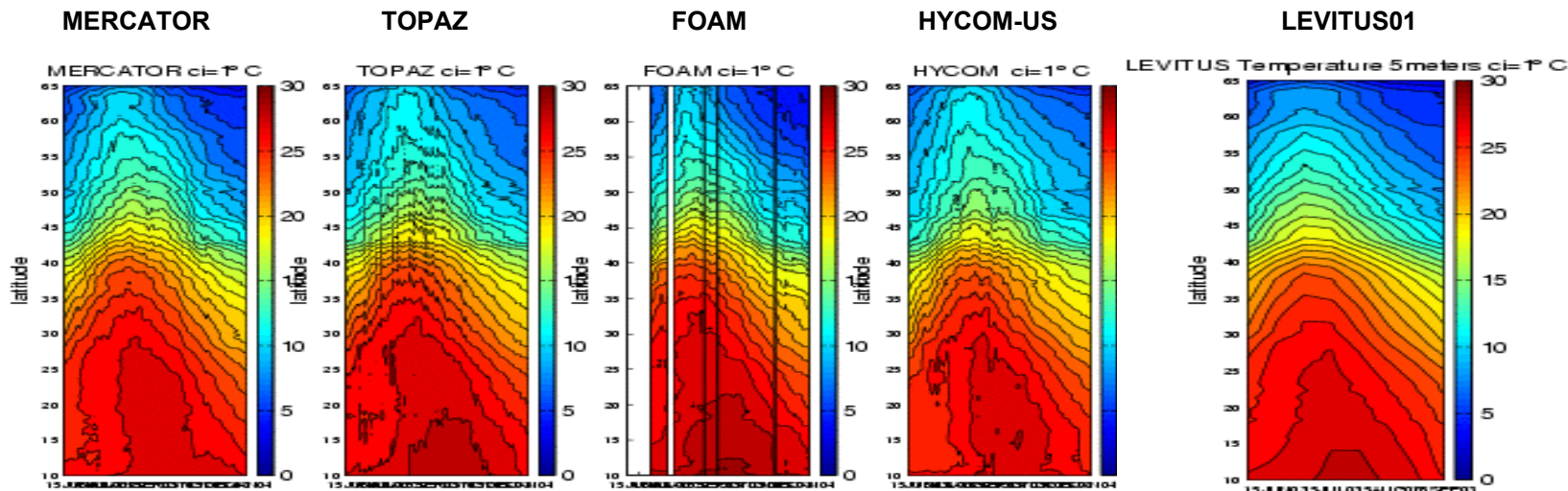
- MODEL-MODEL-CLIMATOLOGY (« Dynamo like »)

Willebrand, J., B. Barnier, C. Böning, C. Dieterich, P.D. Killworth, C. LeProvost, Y. Jia, J.-M. Molines and A.L. New,  
2001: Circulation characteristics in three eddy-permitting models of the North Atlantic.  
[\*Progress in Oceanography\*, 48, 2-3, 123-161.](#)

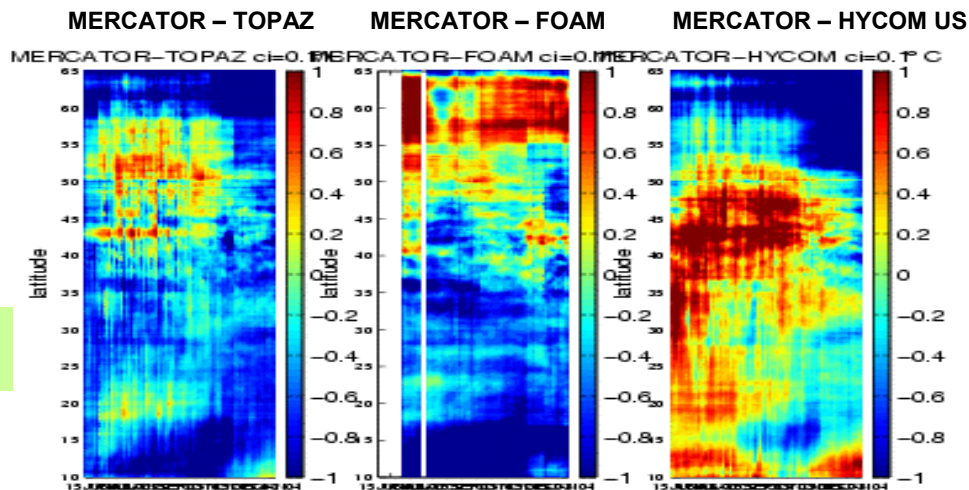
- MODEL-Real time OBSERVATIONS

# Hovmuller plots of ZONAL MEAN SURFACE (5meters) Atlantic TEMPERATURE

ZONAL MEANS

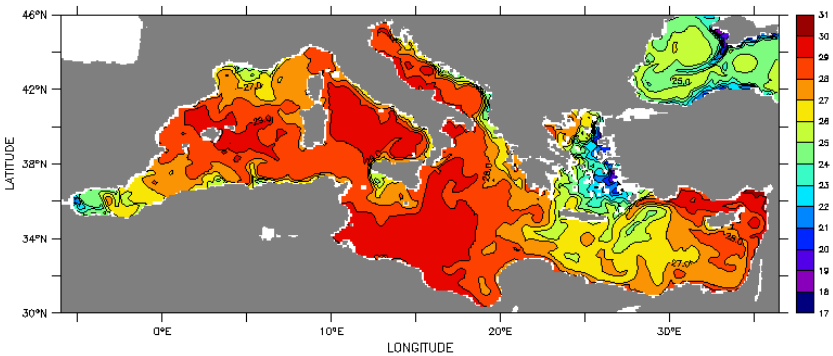


ZONAL MEANS DIFFERENCES



DEPTH (m) : 5  
TIME : 20-AUG-2003 00

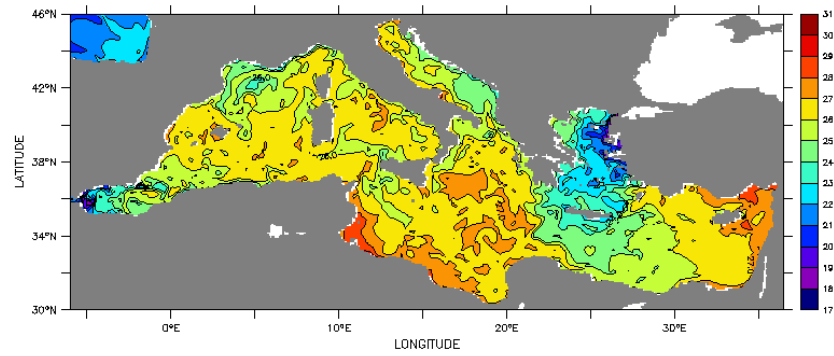
# FOAM



temperature (C)

DEPTH (m) : 5  
TIME : 20-AUG-2003 00

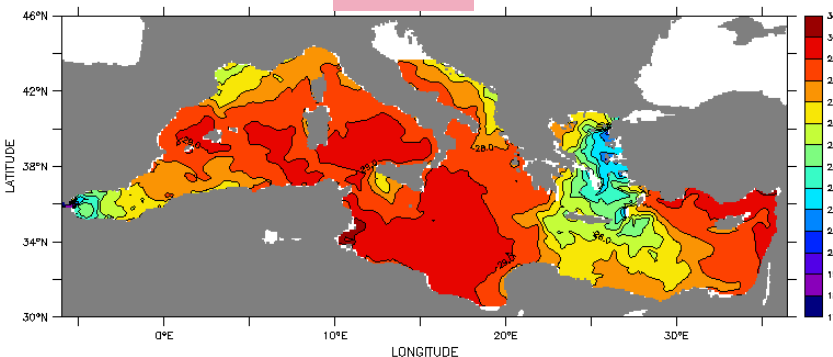
# MERCATOR



temperature (degC)

DEPTH (m) : 5  
TIME : 20-AUG-2003 00

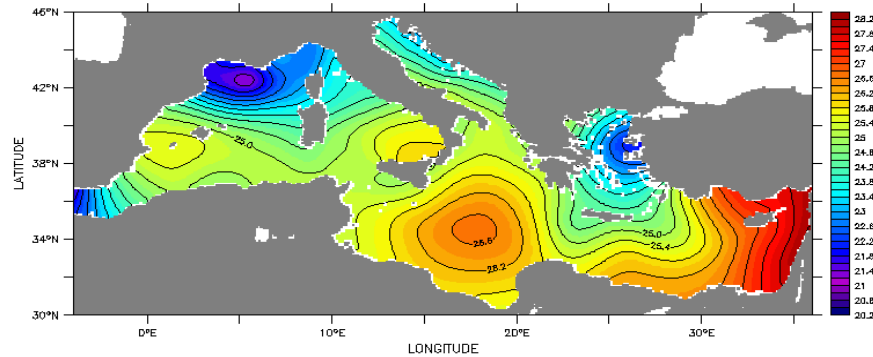
# MFS



temperature (degC)

DEPTH (m) : 5  
TIME : 01-AUG 00

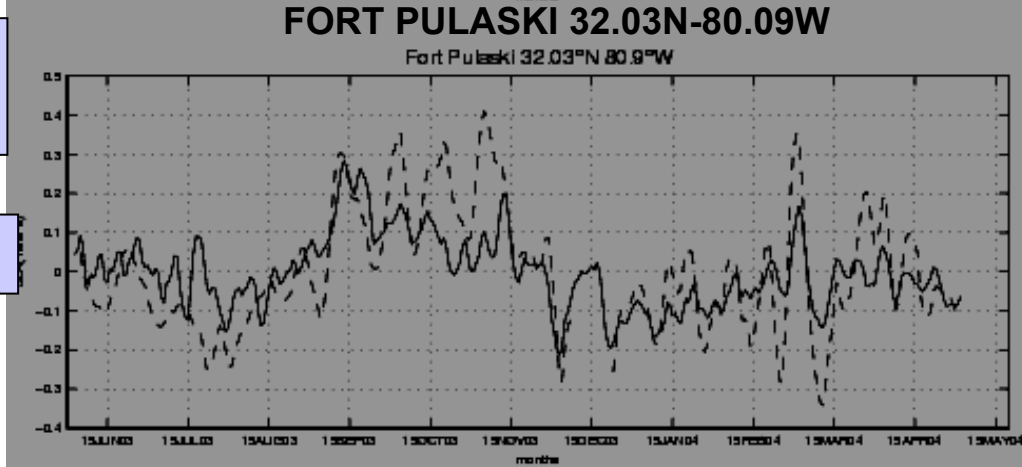
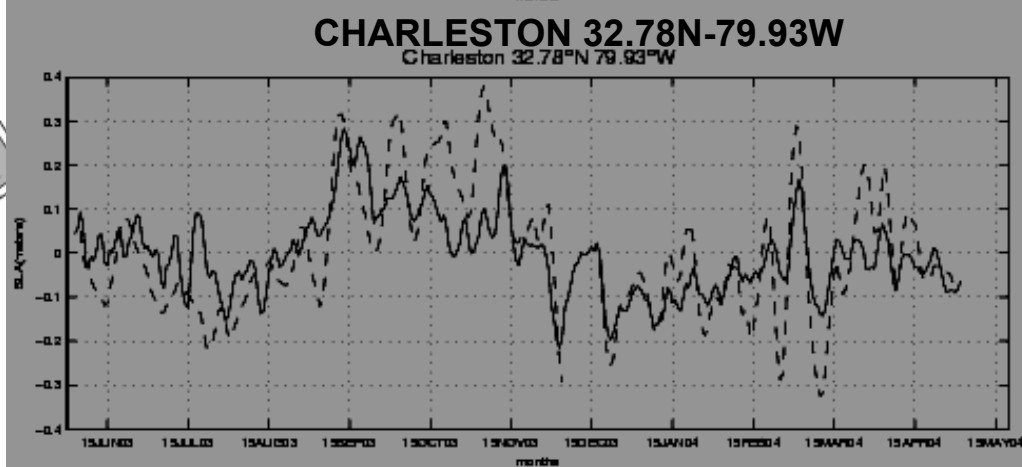
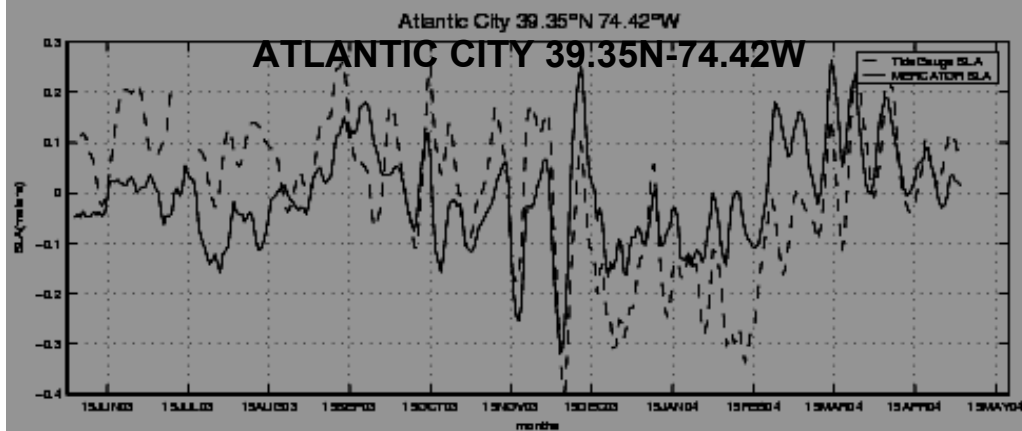
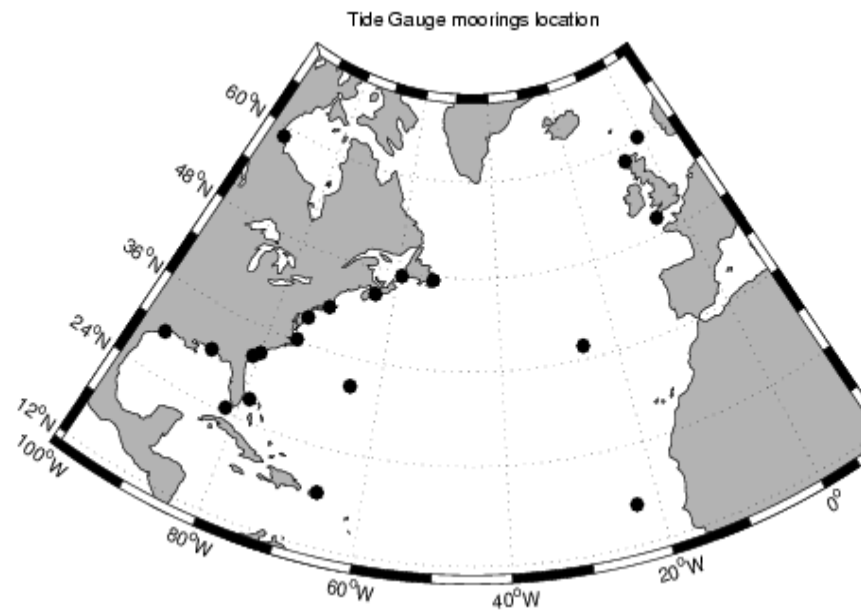
# MEDATLAS



temperature (degC)

## HEAT WAVE EVENT SUMMER 2003

## 5 meters depth TEMPERATURE AUGUST 2003



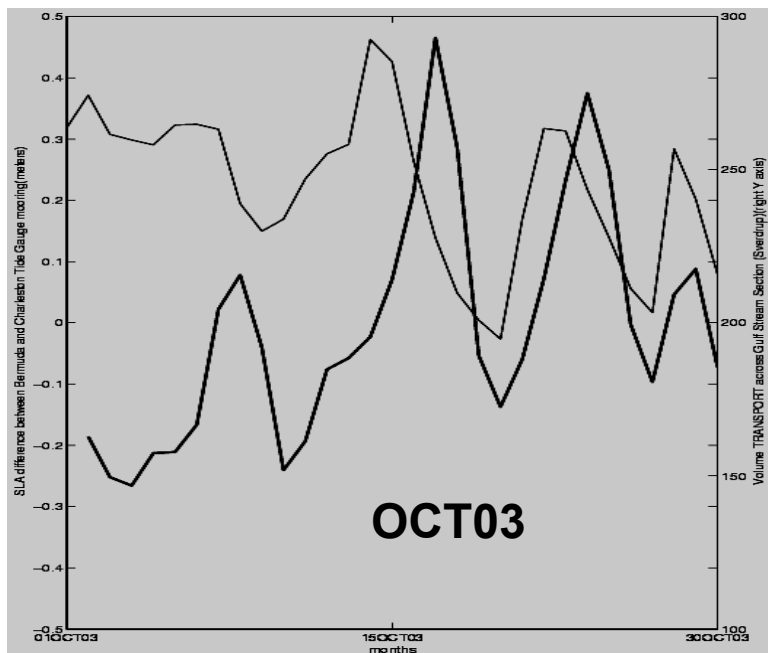
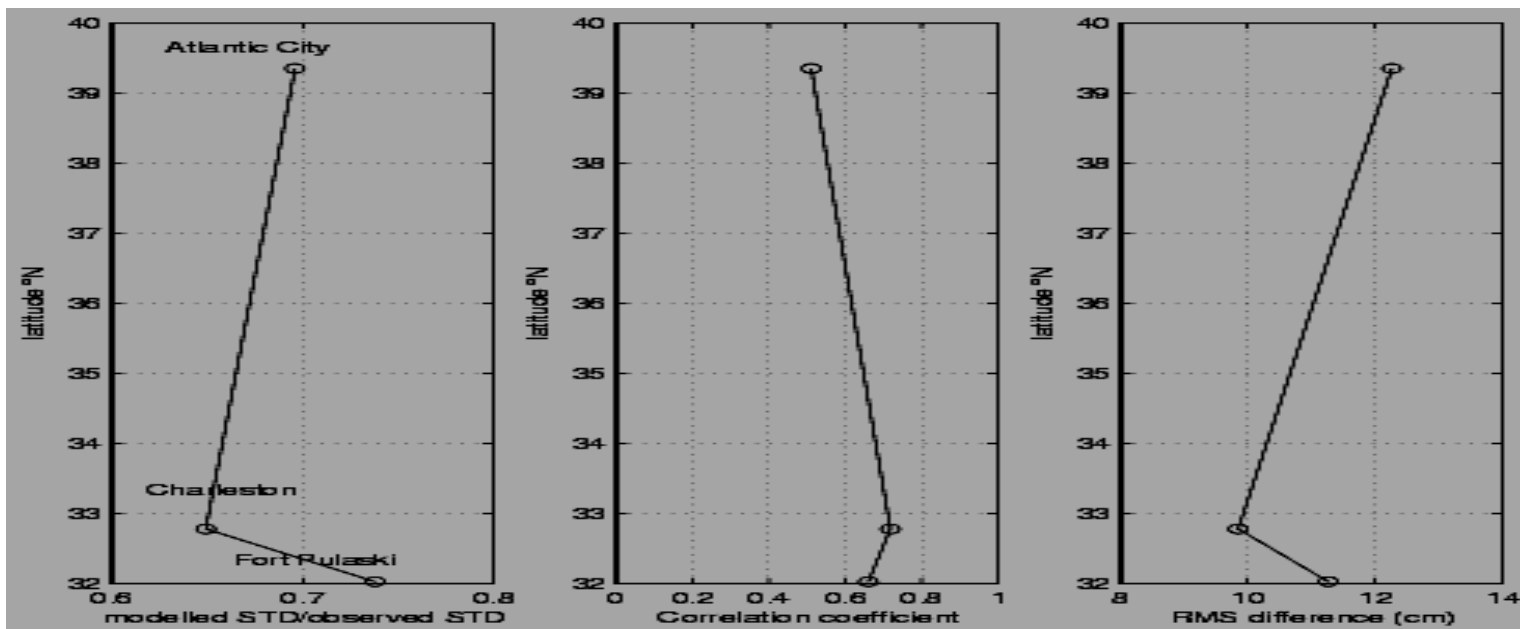
**TIDE GAUGE SLA MEASUREMENTS**  
(not delivered on real time basis)

**No data assimilation in coastal areas**

Modelled STD/Observed STD

Correlation coeff

RMS difference (cm)



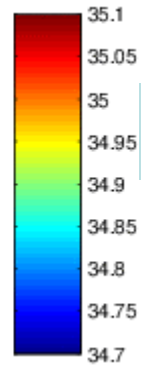
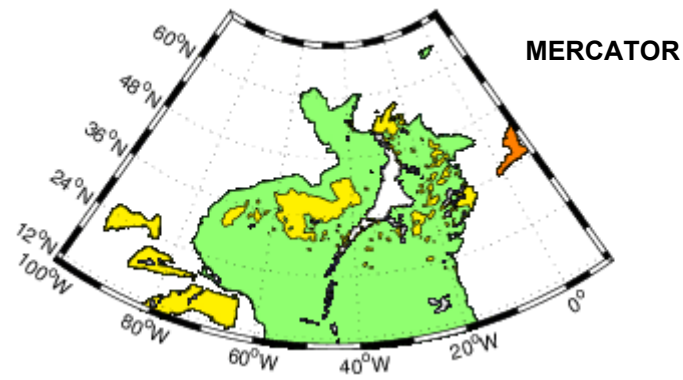
— SLA DIFFERENCE CHARLESTON-BERMUDA

— VOLUME TRANSPORT (MERCATOR) through GS at 30N

- Impact from Spin up length on deep ocean

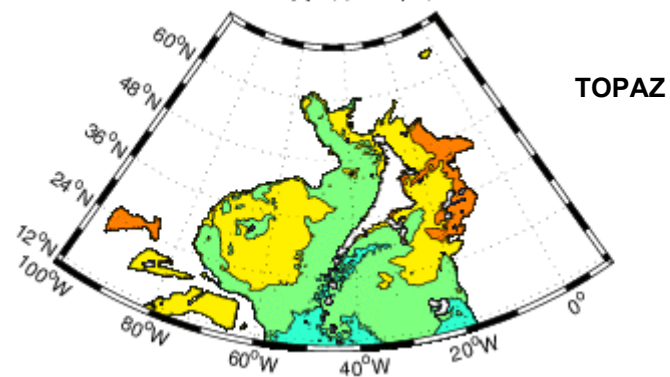
# CLASS1 July mean salinity at 3000m depth (ci=0.05psu)

MERCATOR JUL2003 3000meters Salinity (psu) (ci=0.05psu)MAX=38.4182 MIN=34.9029

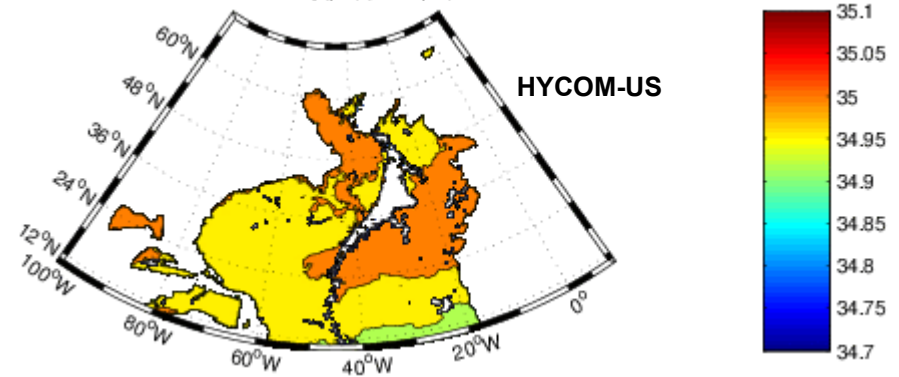


DRIFT from SPIN UP length

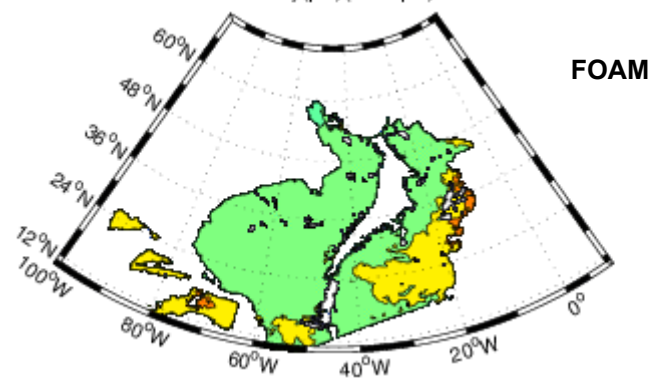
TOPAZ JUL2003 3000meters Salinity (psu) (ci=0.05psu)MAX=35.2507 MIN=34.8642



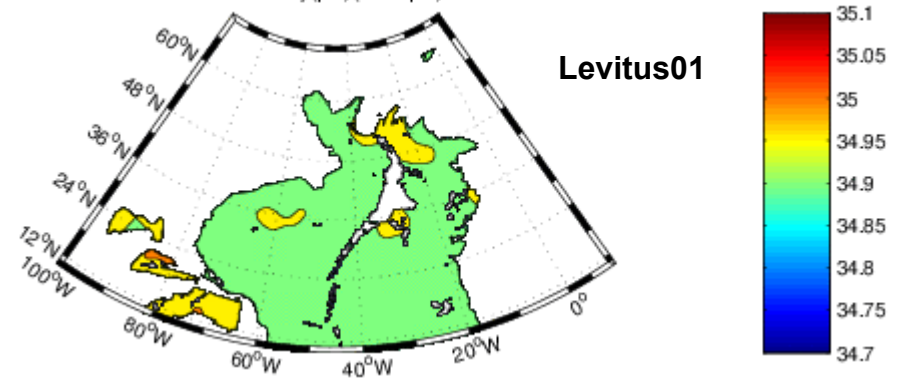
HYCOM-US JUL2003 3000meters Salinity (psu) (ci=0.05psu)MAX=36.1972 MIN=34.9139



FOAM JUL2003 3000meters Salinity (psu) (ci=0.05psu)MAX=38.9605 MIN=34.883



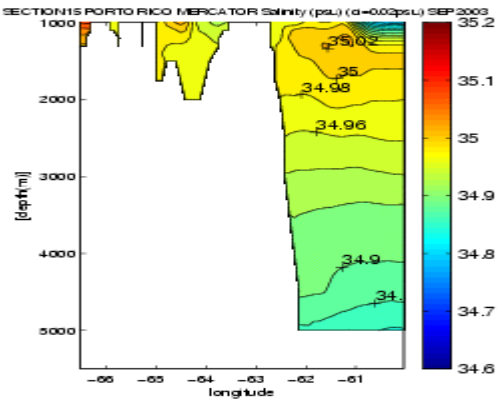
LEVITUS2001 JUL 3000meters Salinity (psu) (ci=0.05psu)MAX=35.0179 MIN=34.8895



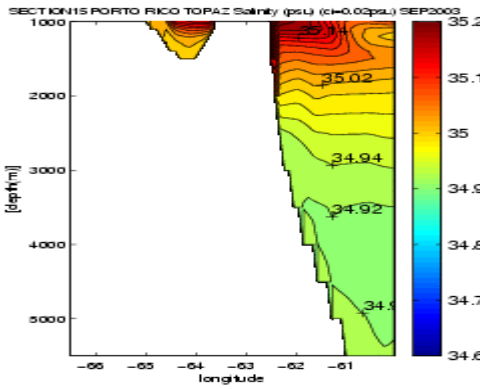


# Salinity DWBC at 17°N

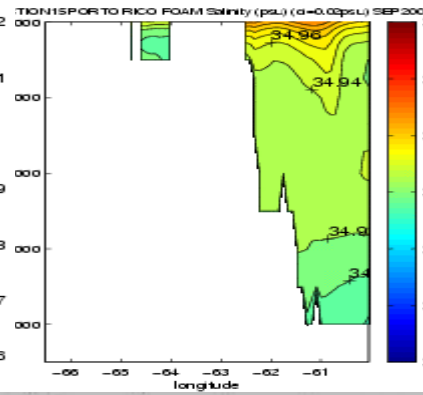
## MERCATOR



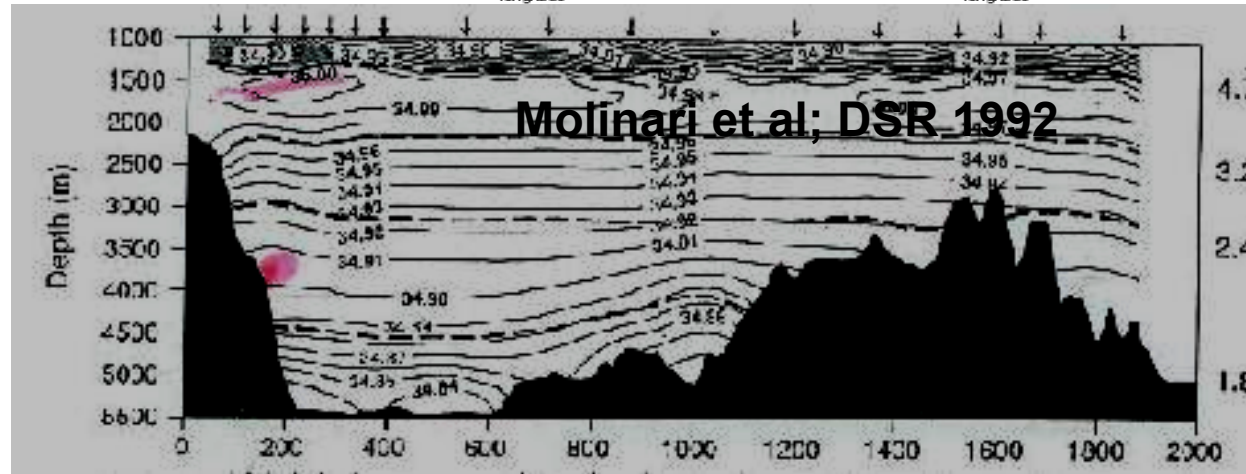
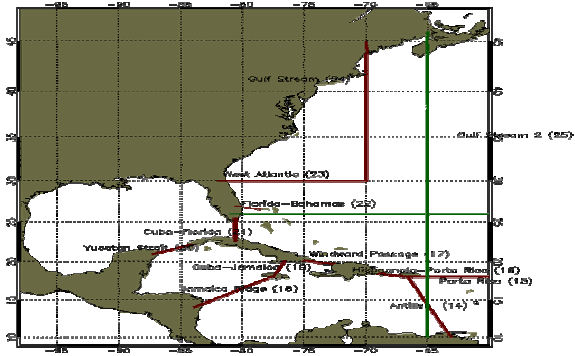
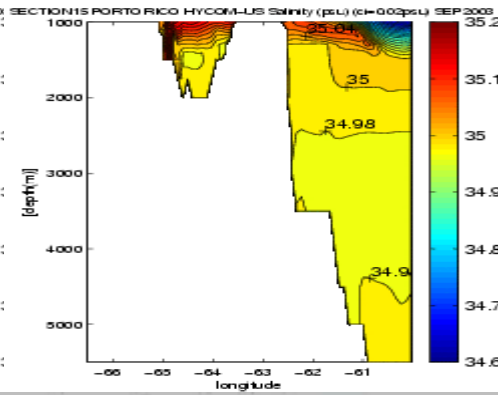
## TOPAZ



## FOAM

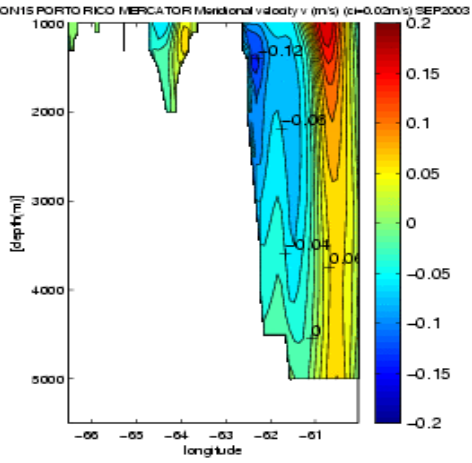


## HYCOM-US

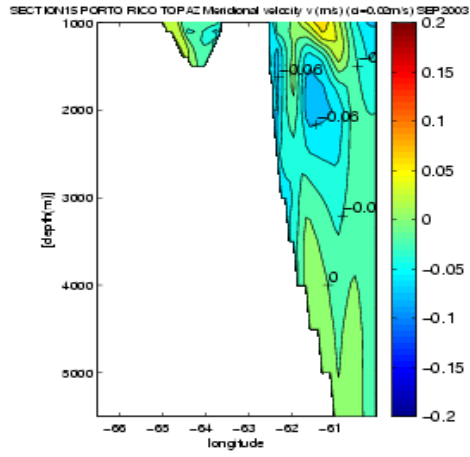


# SEP03- Meridional Velocity DWBC at 17°N

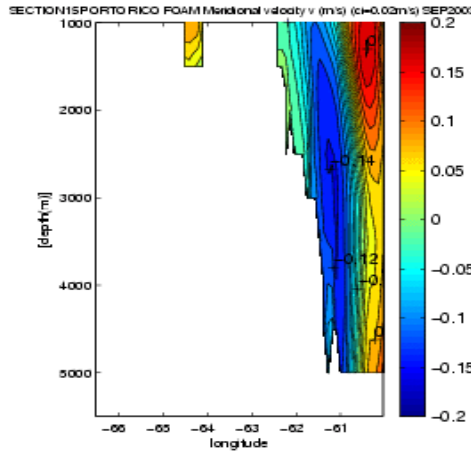
## MERCATOR



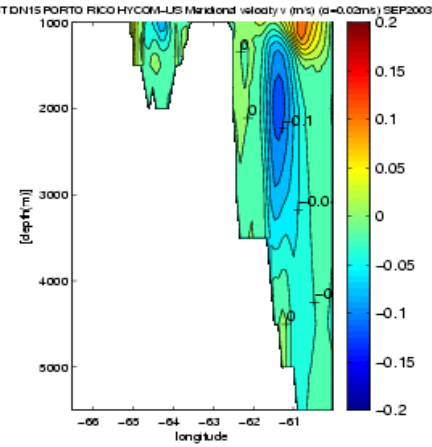
## TOPAZ



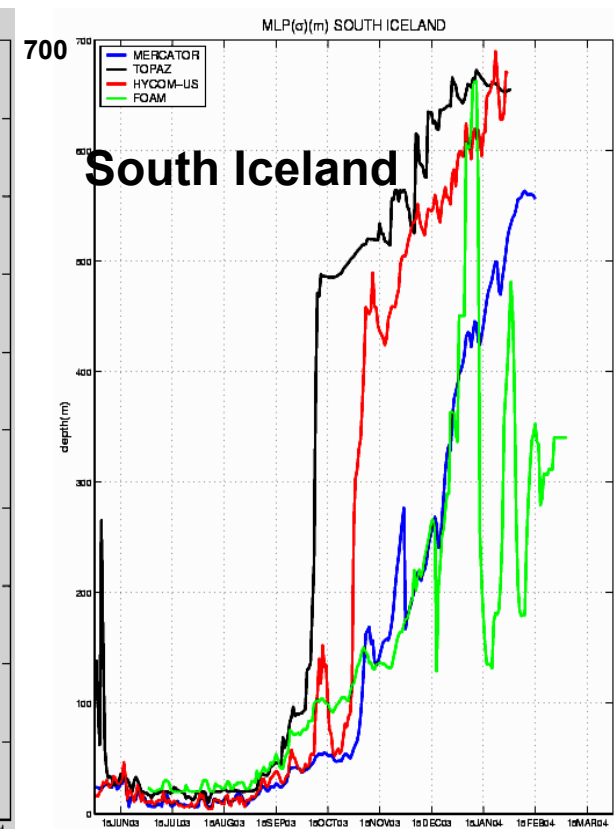
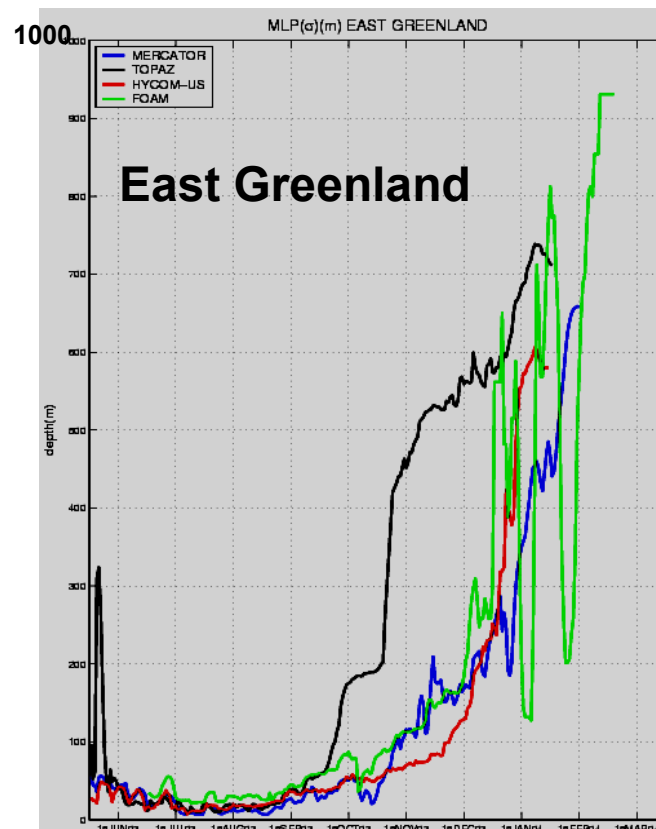
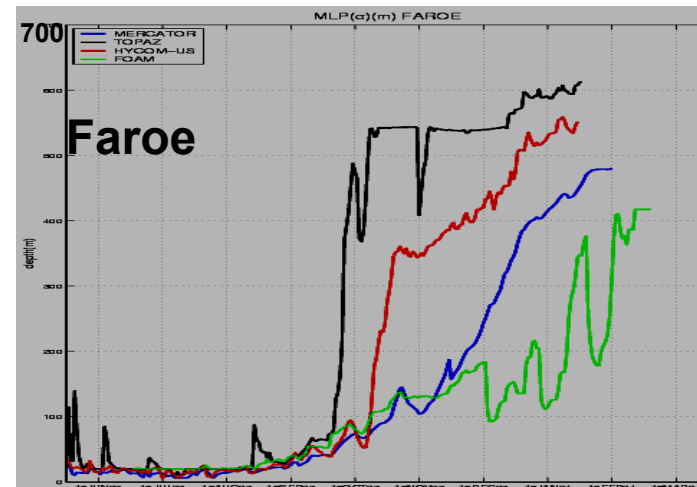
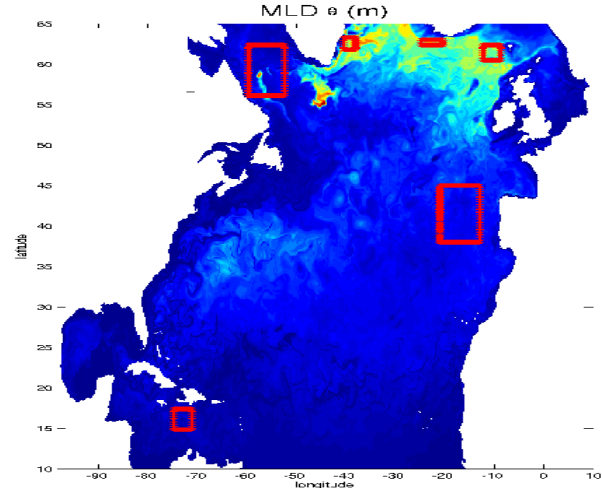
## FOAM



## HYCOM US

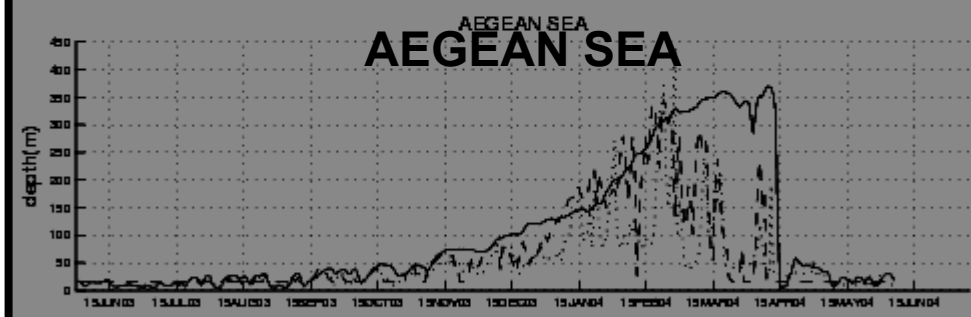
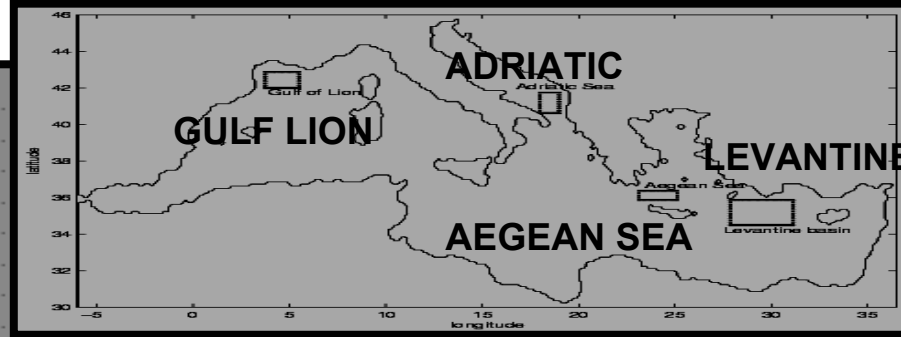
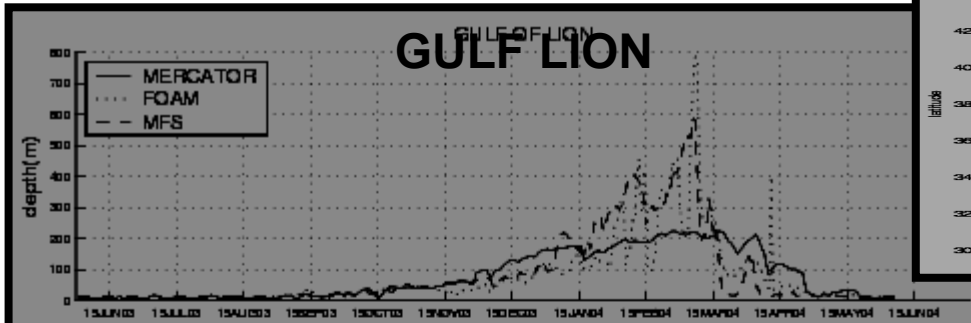


- Impact from Mixing Parameterization



JUNE 1st 03

APR 1st 04



**Convection Zones  
 in Mediterranean Sea**

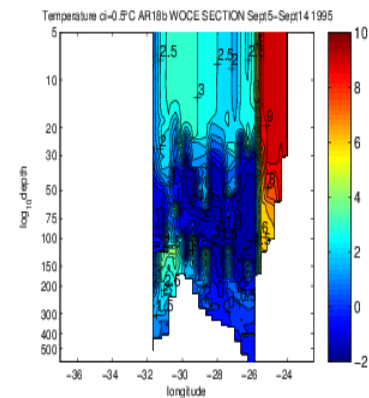
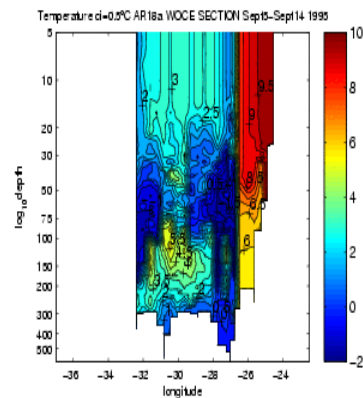
JUNE 1st 03

JUNE 1st 04

- Impact from Ice Model and assimilation of ice concentration not clear.

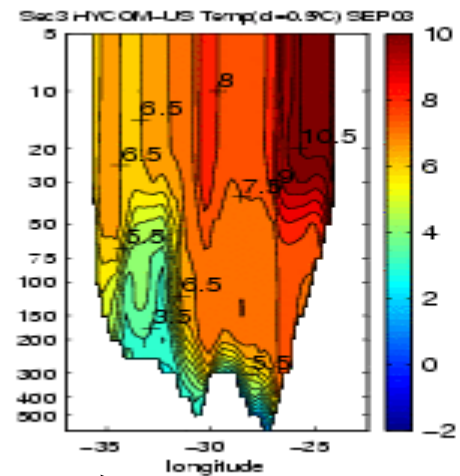
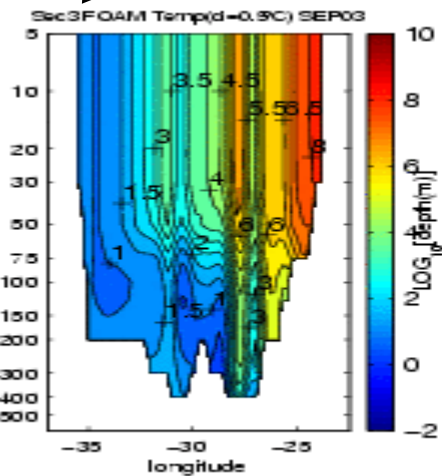
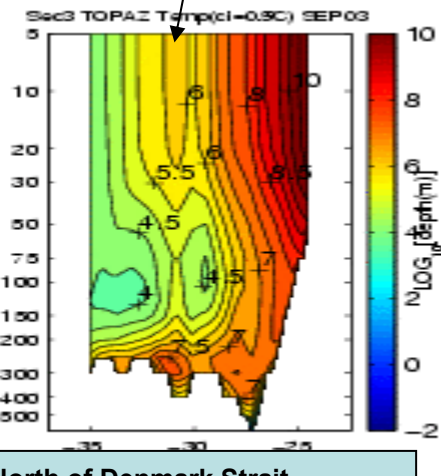
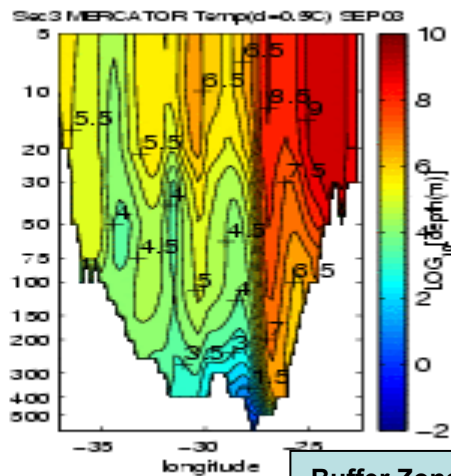
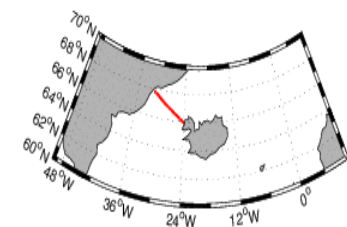
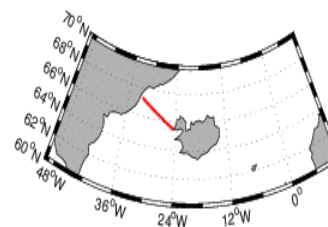
→ Need for New insight from Mersea-IP :  
Arctic Ocean included

# Denmark Strait Section Potential Temperature



## WOCE

Ice model+  
Ice concentration assimilation



Buffer Zone North of Denmark Strait  
With Relaxation to Climatology

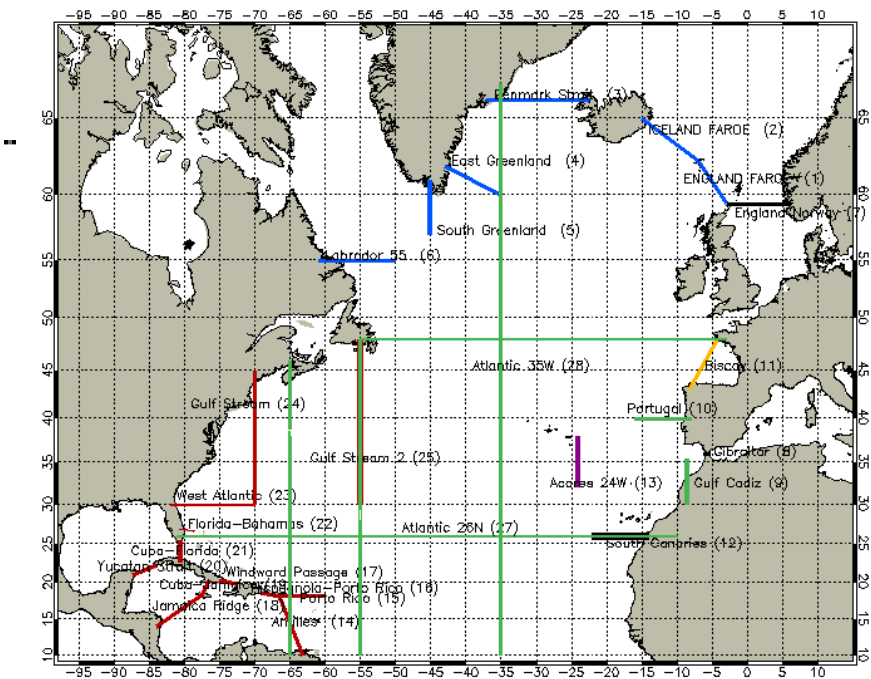
MERCATOR

TOPAZ

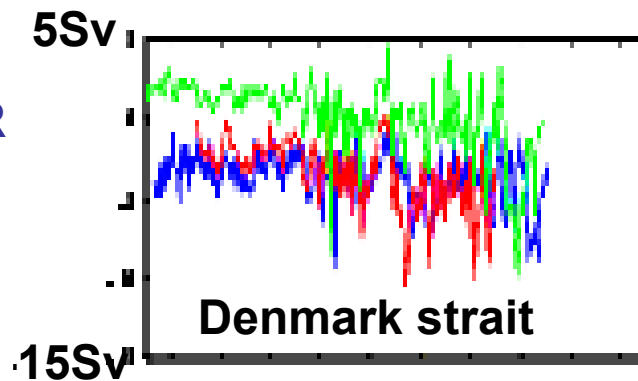
FOAM

HYCOM-US

# OVERFLOWS SECTIONS TOTAL VOLUME TRANSPORTS



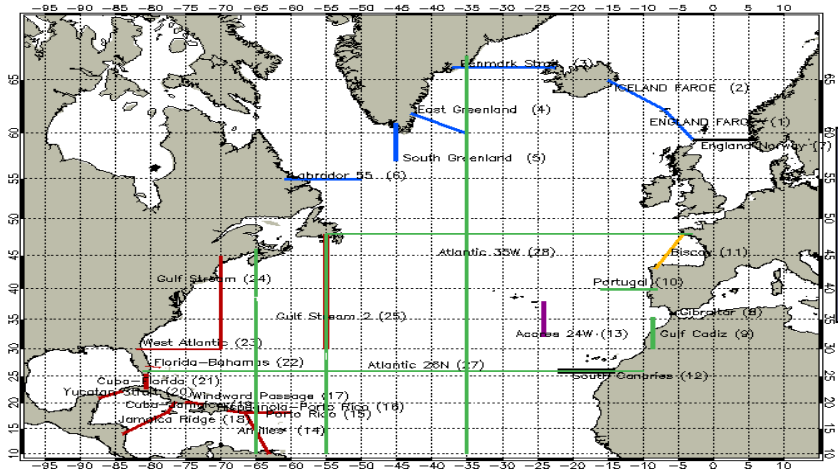
MERCATOR  
FOAM  
TOPAZ



JUNE 1st 03

FEB 1st 04





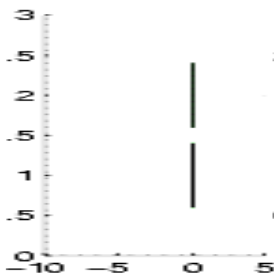
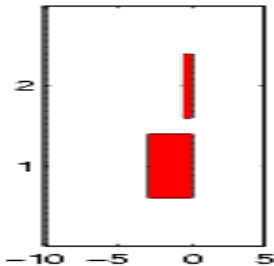
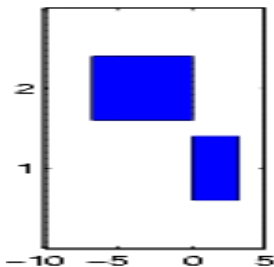
**OVERFLOWS SECTIONS  
VOLUME TRANSPORTS  
per density class**

Denmark strait

JUN03-JAN04 MEAN

$25 \leq \rho \leq 27.8$

$27.8 \leq \rho \leq 29$



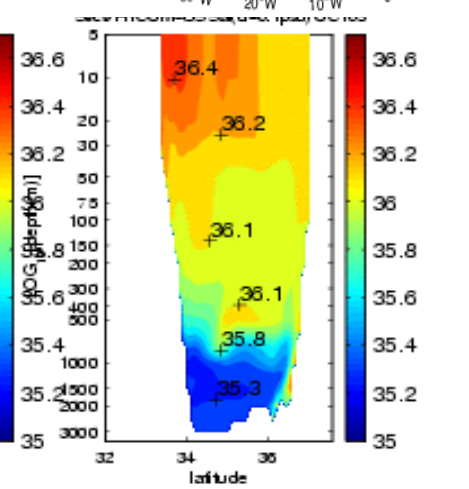
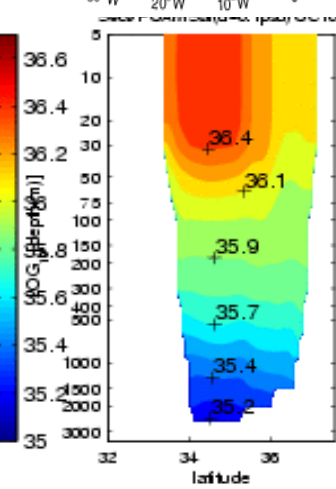
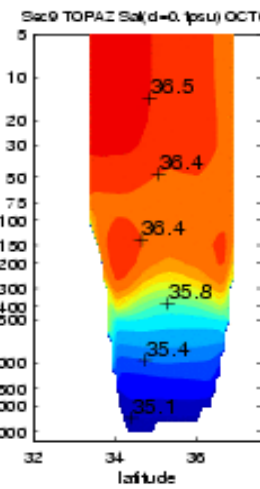
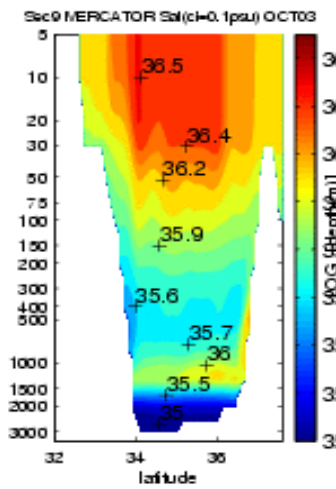
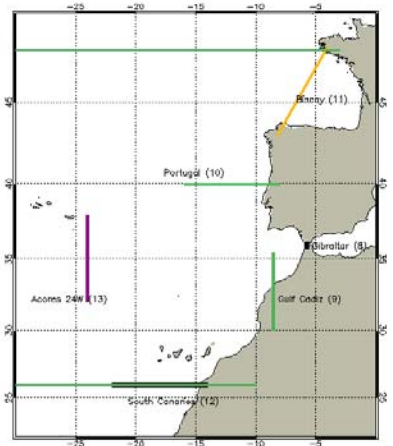
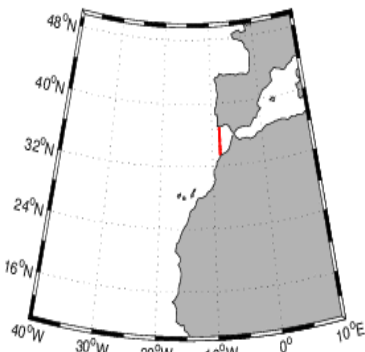
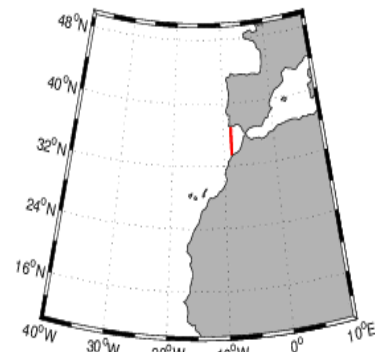
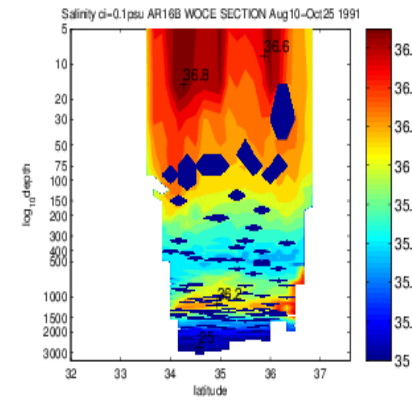
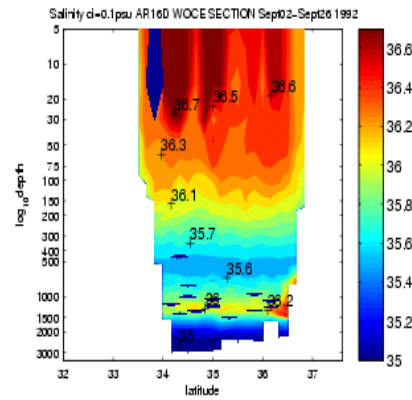
MERCATOR  
FOAM  
TOPAZ

- Impact from  
Mediterranean Outflow Water relaxation  
Or MOW entrainment parameterization

# Gulf Cadiz Section 9°W Salinity

WOCE AR16D SEP 1992

WOCE AR16B AUG OCT 1991



MERCATOR

TOPAZ

FOAM

HYCOM

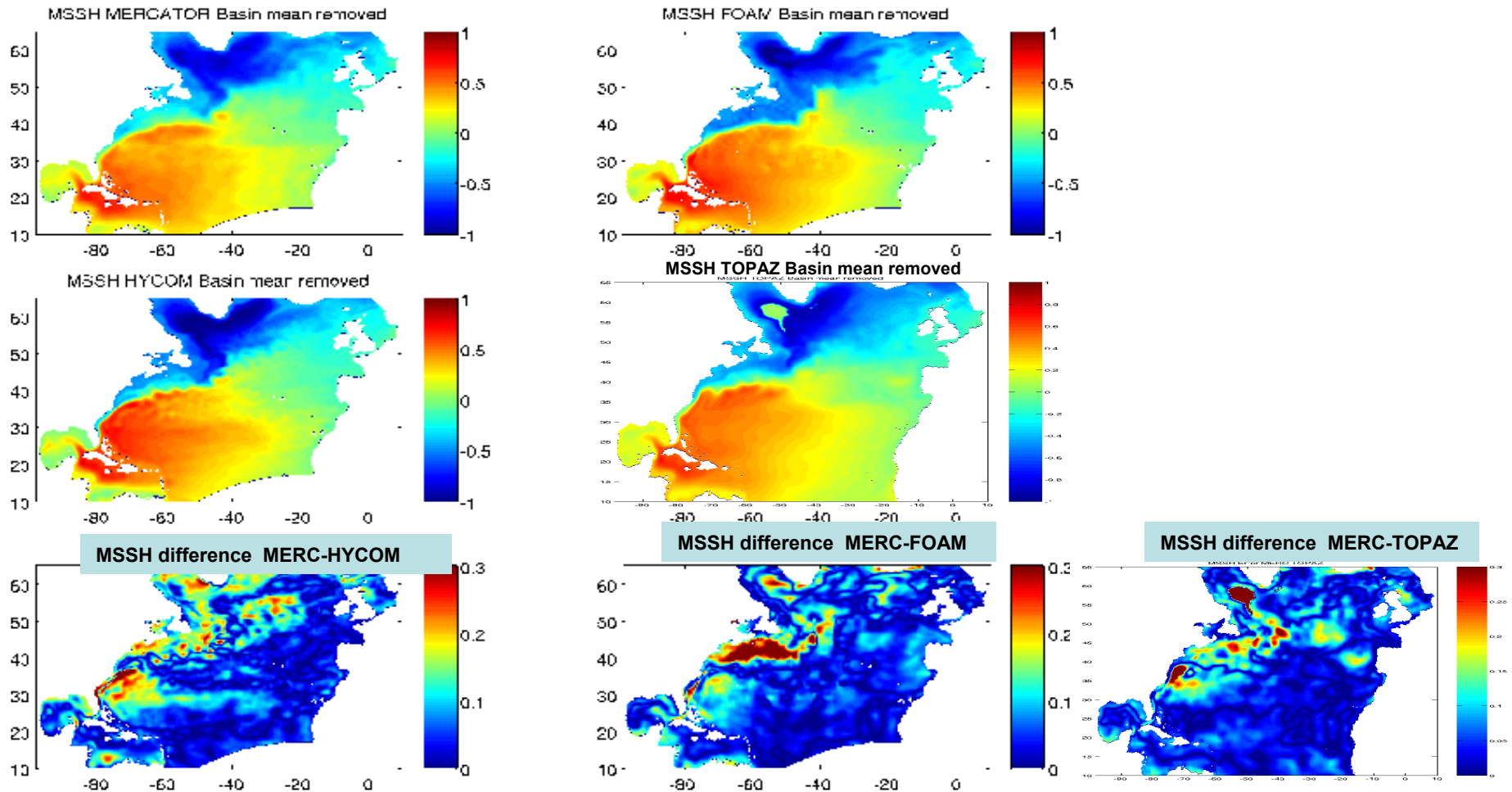
- Impact from MSSH  
(Mean Sea Surface Height)  
used as a reference  
for Data Assimilation

# Mean Sea Surface Height (MSSH) (in meters)

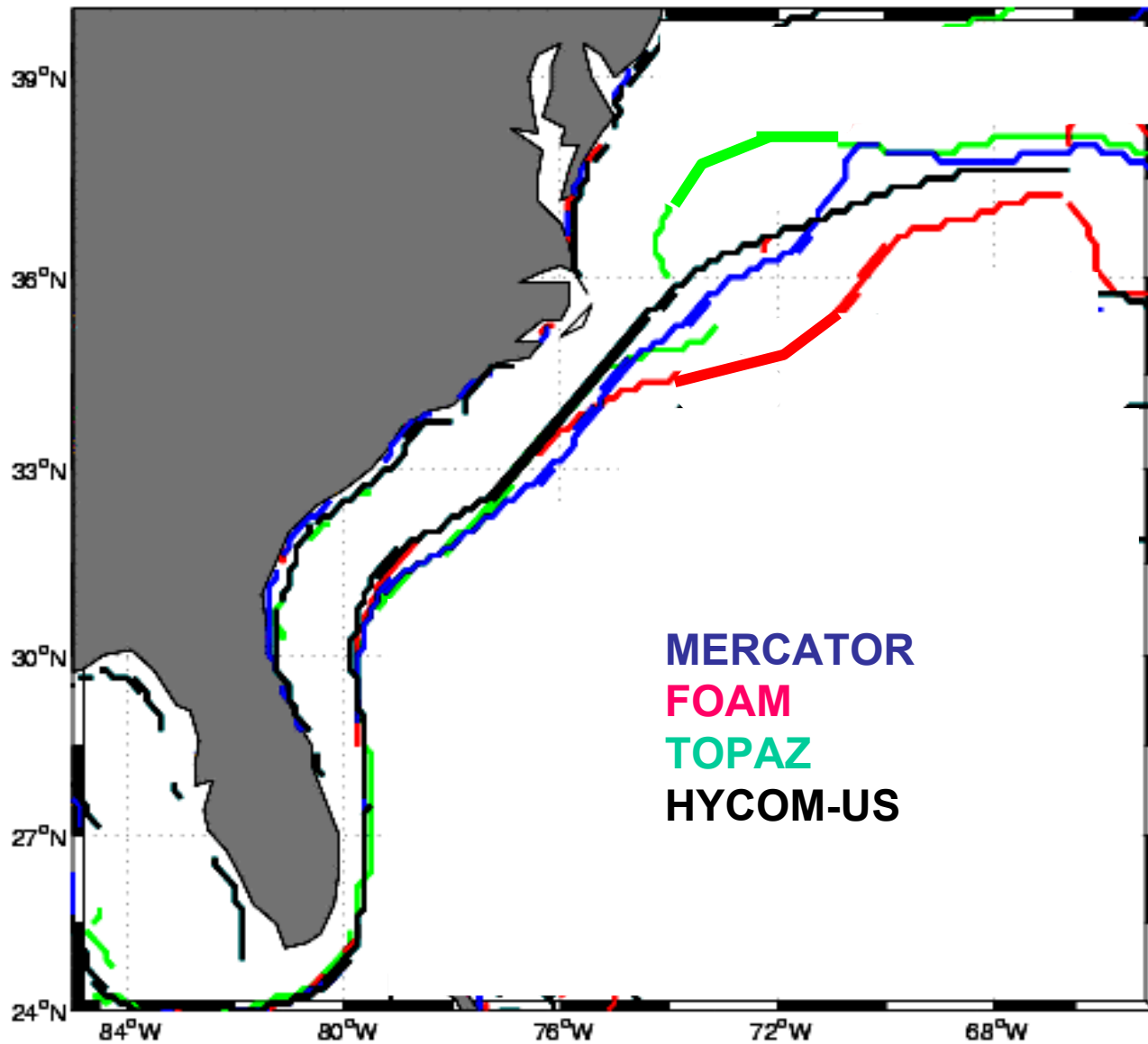
# Basin Mean Removed

- MERCATOR → MSSH based on gravity, altimetry and In Situ observations, (Rio et al.)
- FOAM → MSSH based on previous run + observations in GS (Singh & Kelly)
- TOPAZ → MSSH based on previous run
- HYCOM → MSSH based on previous 1/12° MICOM free run (ECMWF)

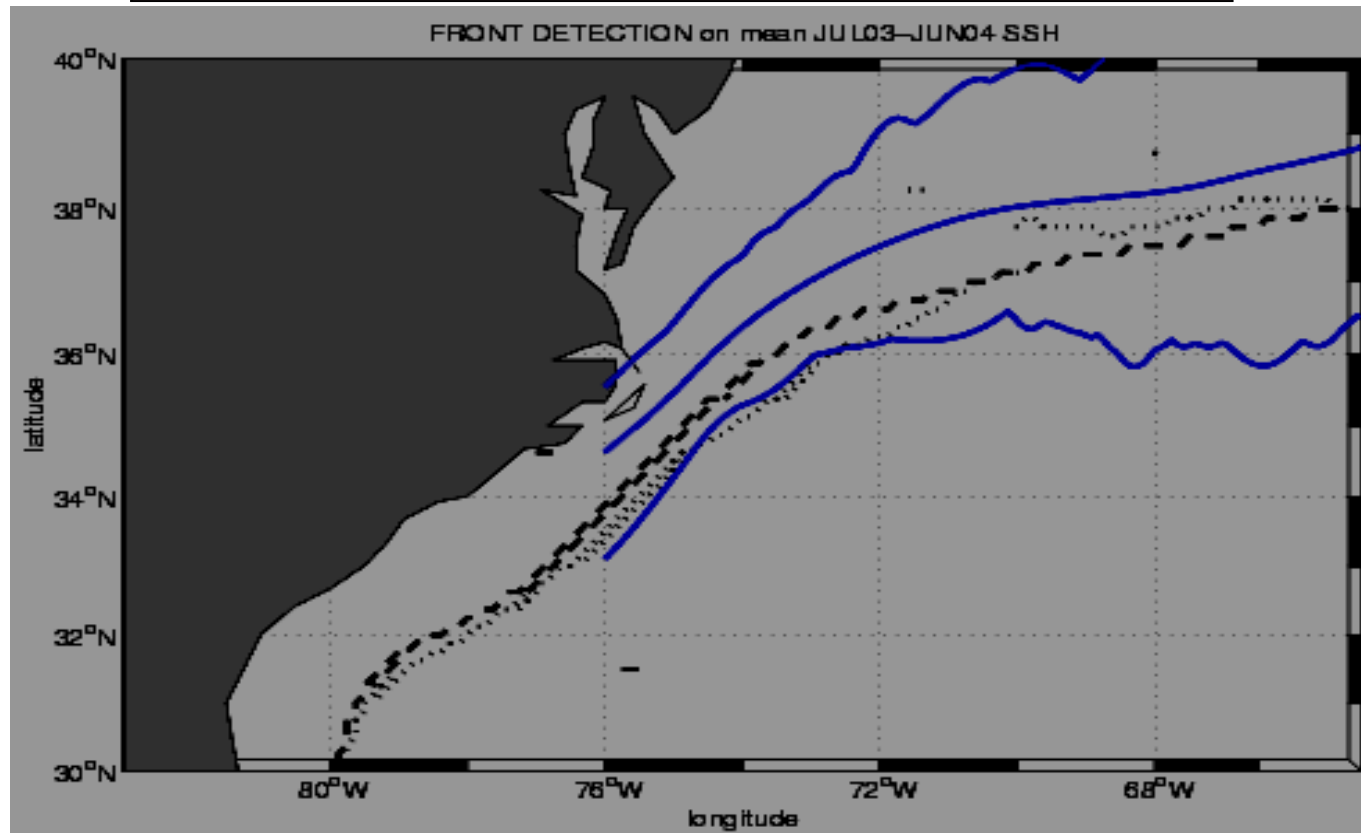
**Birol et al. 2004 : Hard to judge which MSSH is best for assimilation (depends on region considered).**



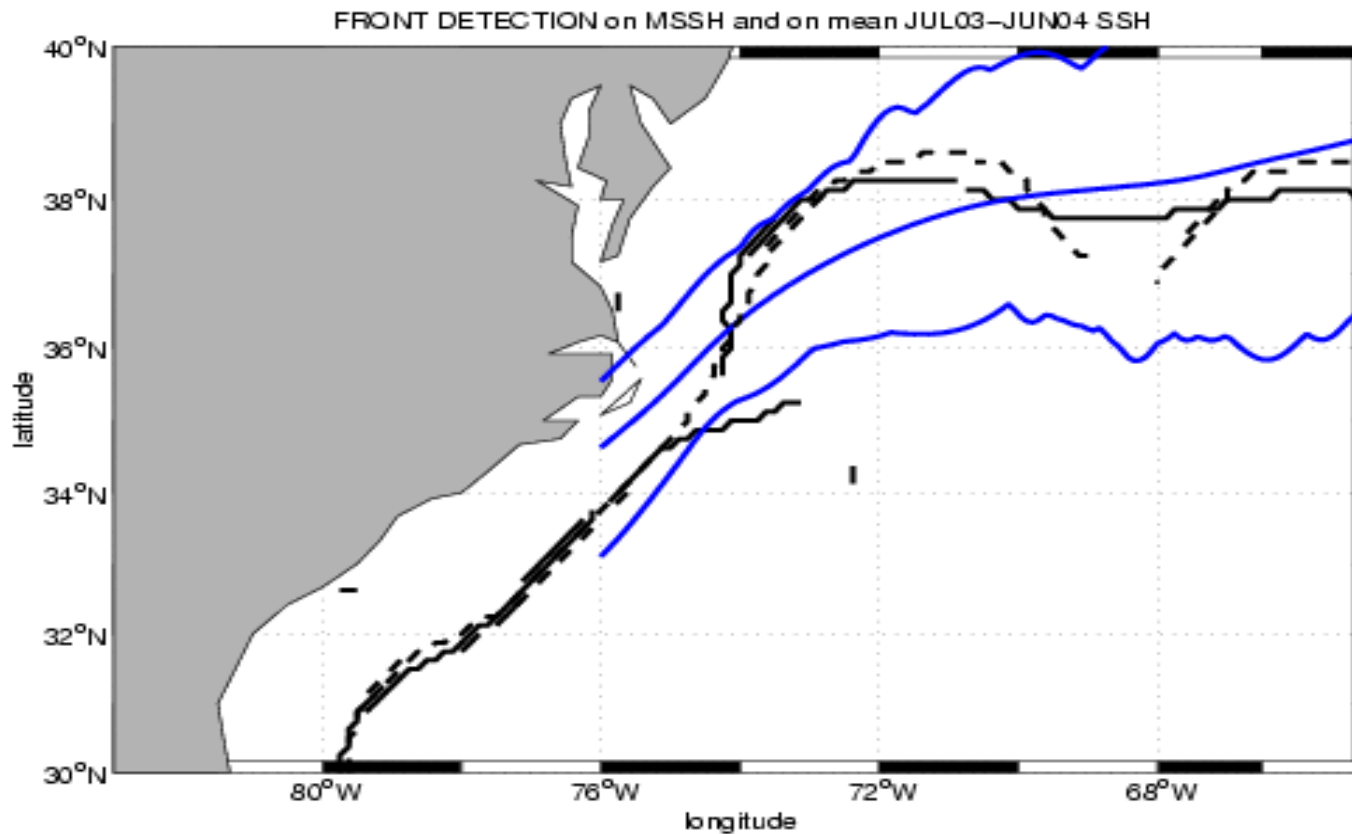
# FRONT DETECTION for mean JUL-DEC 03 SSH



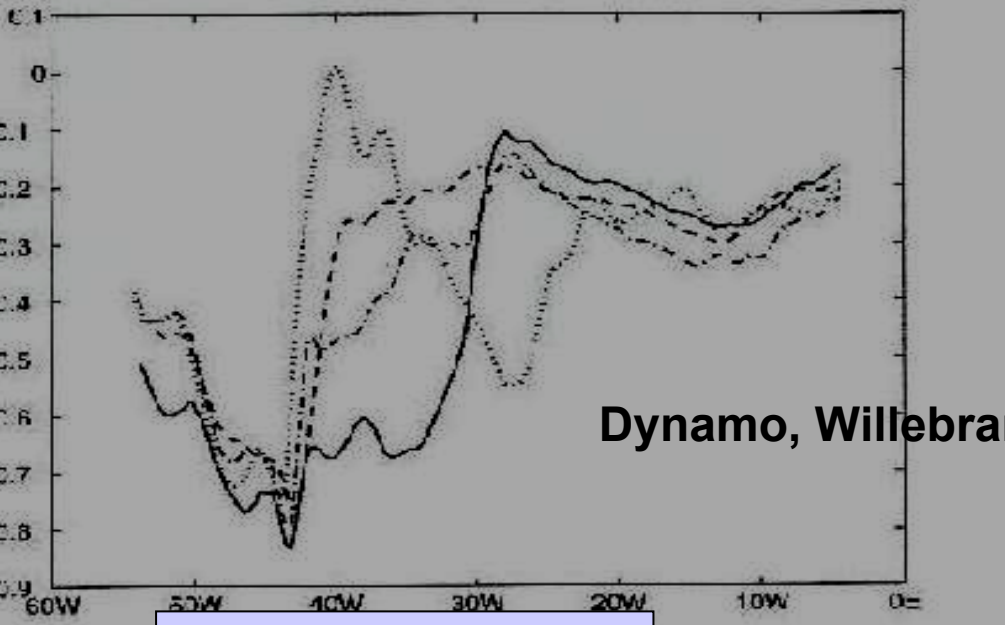
**FRONT DETECTION**  
for mean JUL03-JUN 04 SSH  
**MERCATOR (dotted line)**  
**HYCOM-US (dashed line)**



**FRONT DETECTION**  
for mean JUL03-JUN 04  
SSH TOPAZ (solid line)  
MSSH TOPAZ (dashed line)

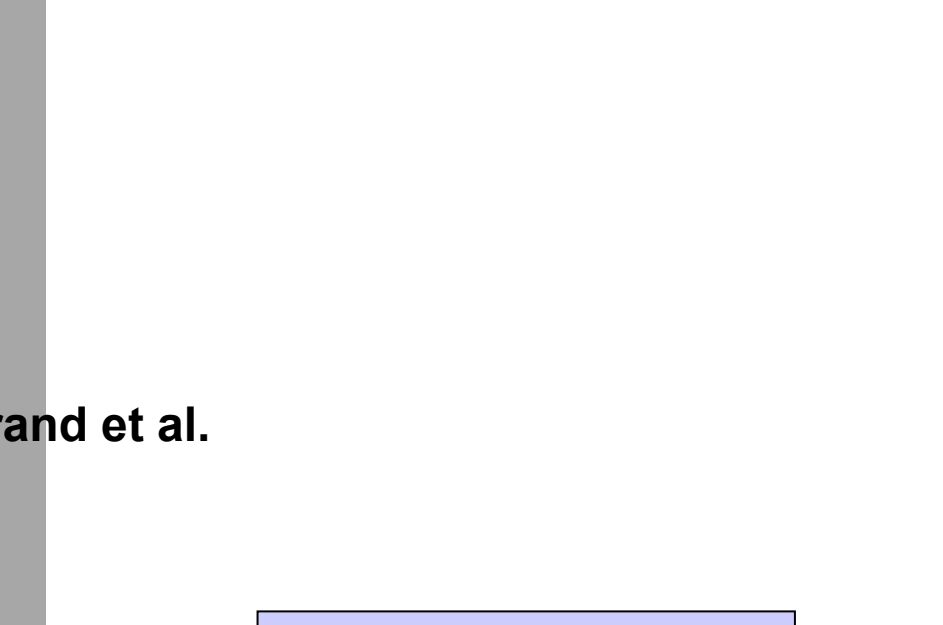




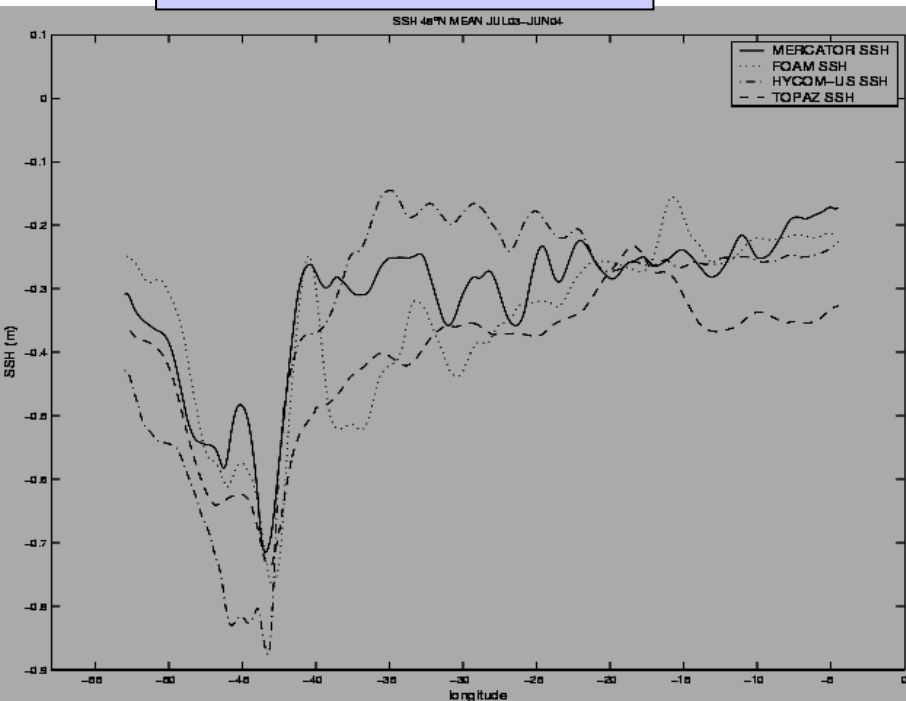


Dynamo, Willebrand et al.

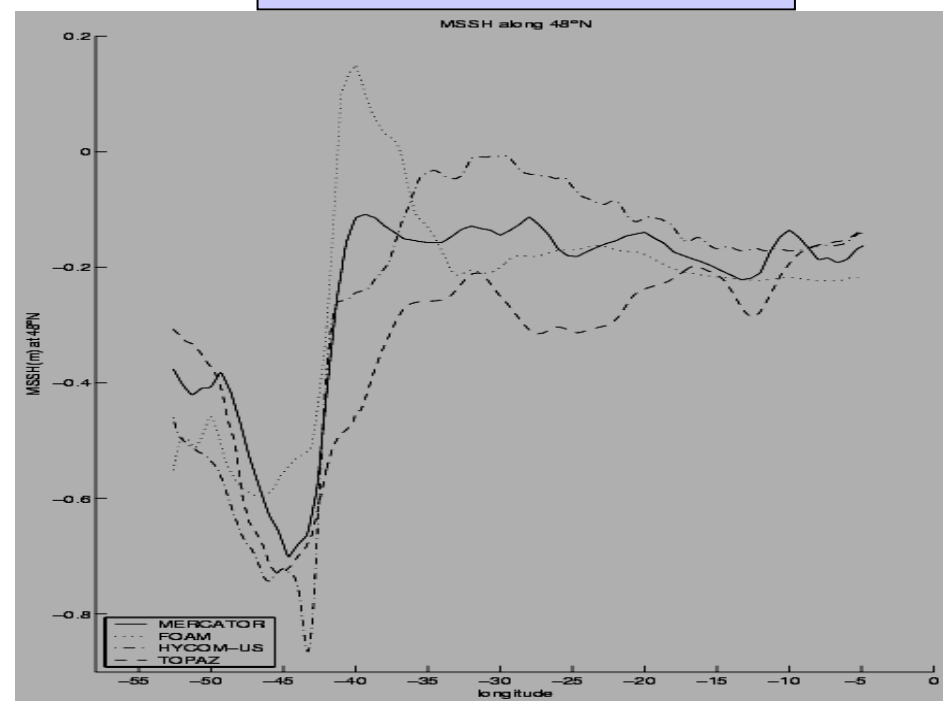
SSH section at 48°N



MSSH section at 48°N



longitude

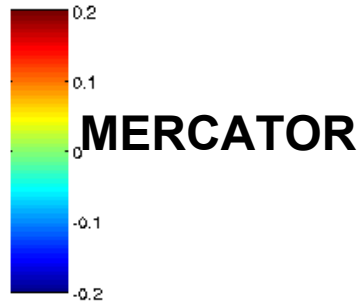
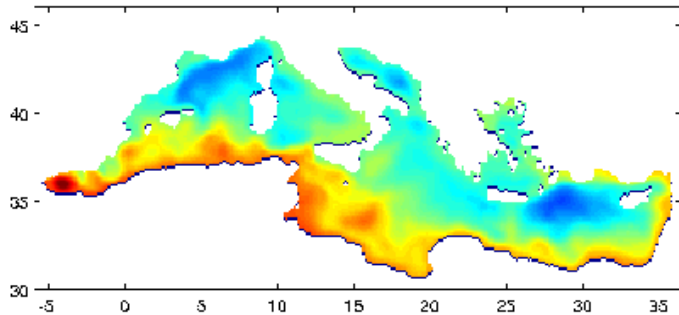


longitude

# IMPACT OF MEAN SEA SURFACE HEIGHT(MSSH) ON MEDITERRANEAN CIRCULATION

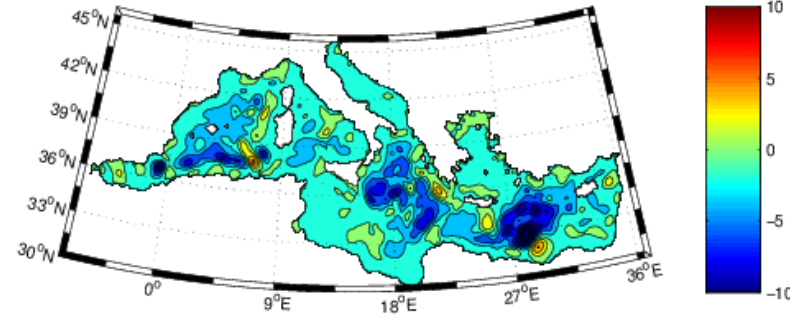
MSSH

MSSH MERCATOR Basin mean removed

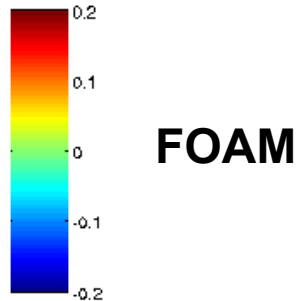
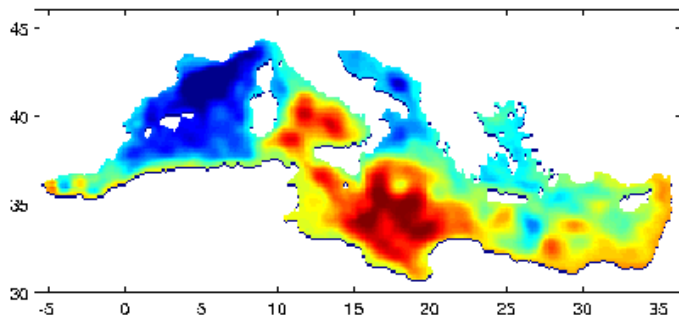


BAROTROPIC STREAM FUNCTION (DEC03)

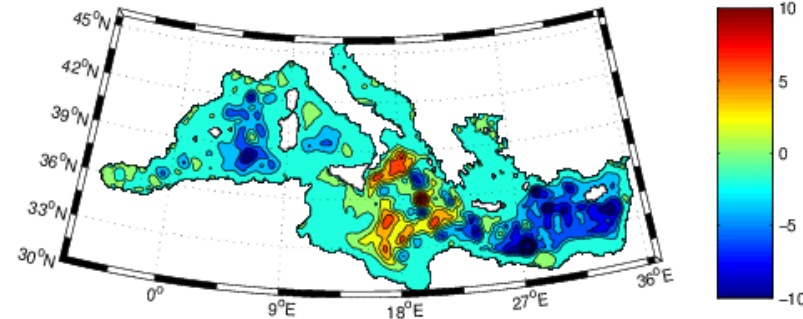
MERCATOR DEC2003 Barotropic Stream Function (Sv) (ci=2Sv)MAX=6.4893 MIN=-23.0886



MSSH FOAM Basin mean removed

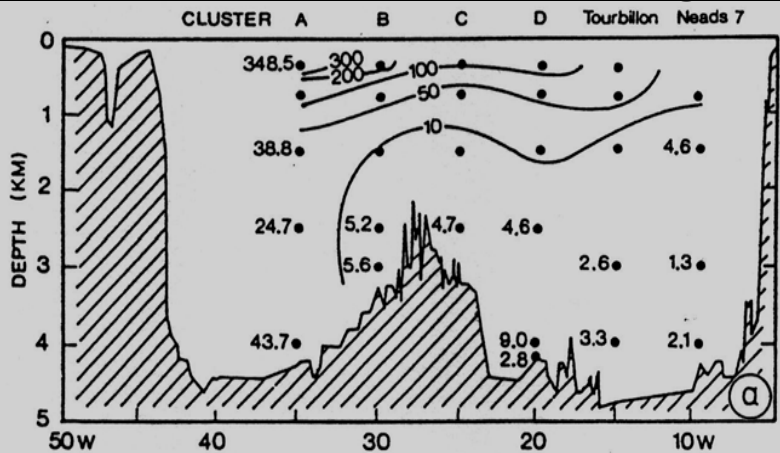


FOAM DEC2003 Barotropic Stream Function (Sv) (ci=2Sv)MAX=12.7075 MIN=-15.9105



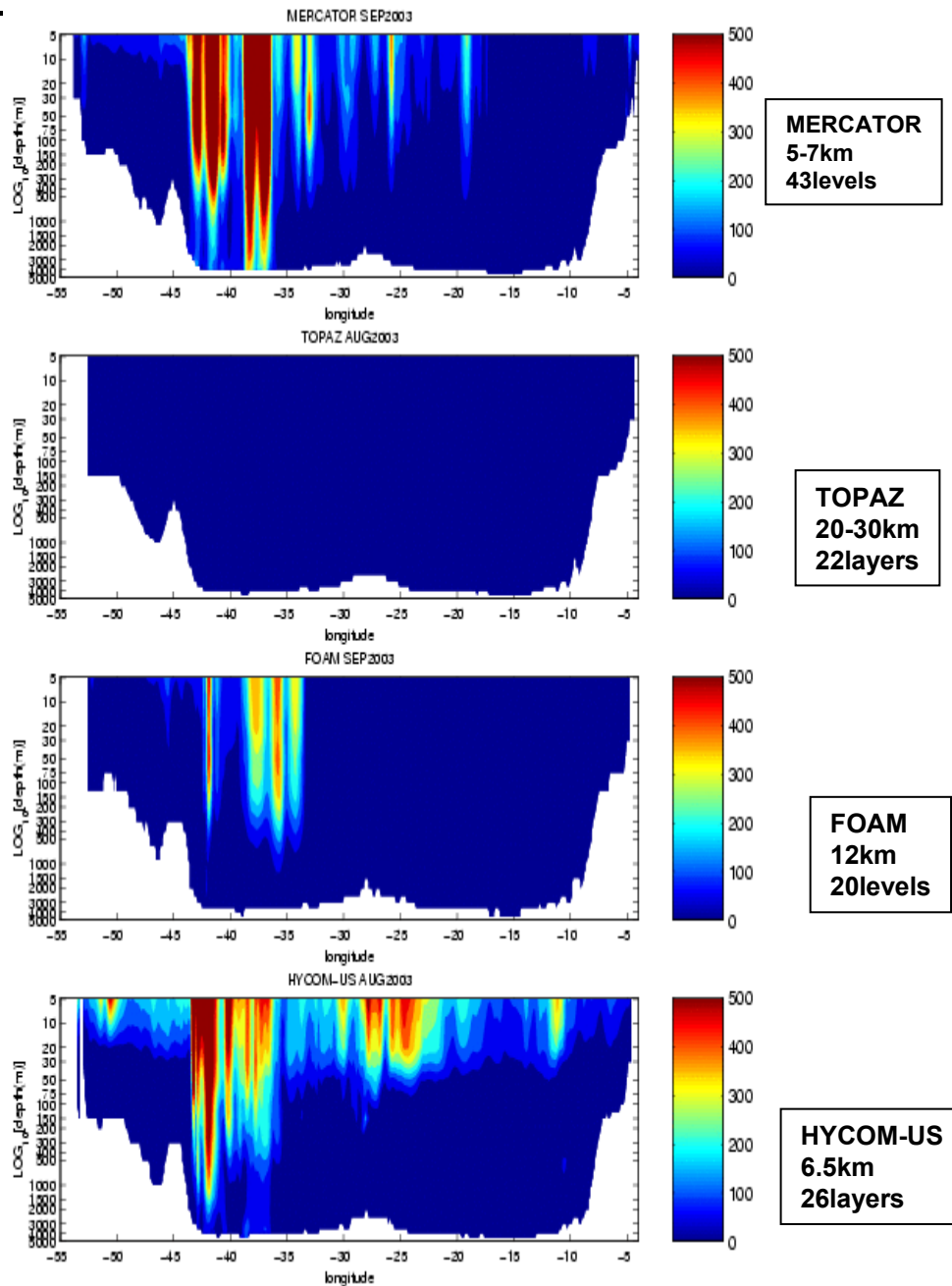
- Impact from horizontal resolution

# Vertical EKE distribution along 48 ° N



EKE estimated from current meter moorings  
Colin de Verdiere et al. 1989

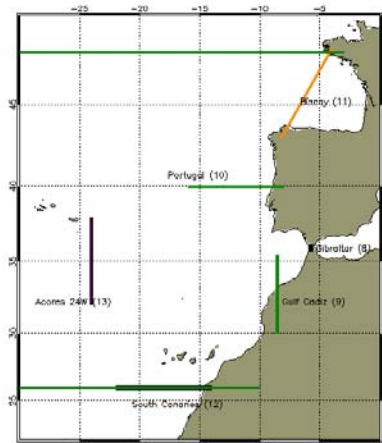
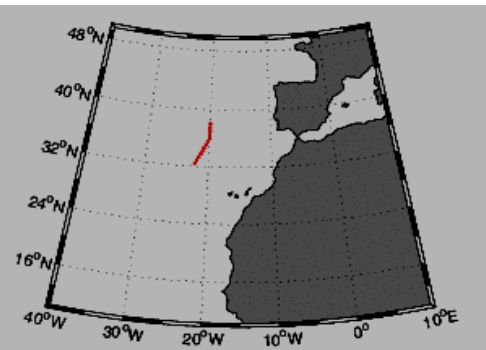
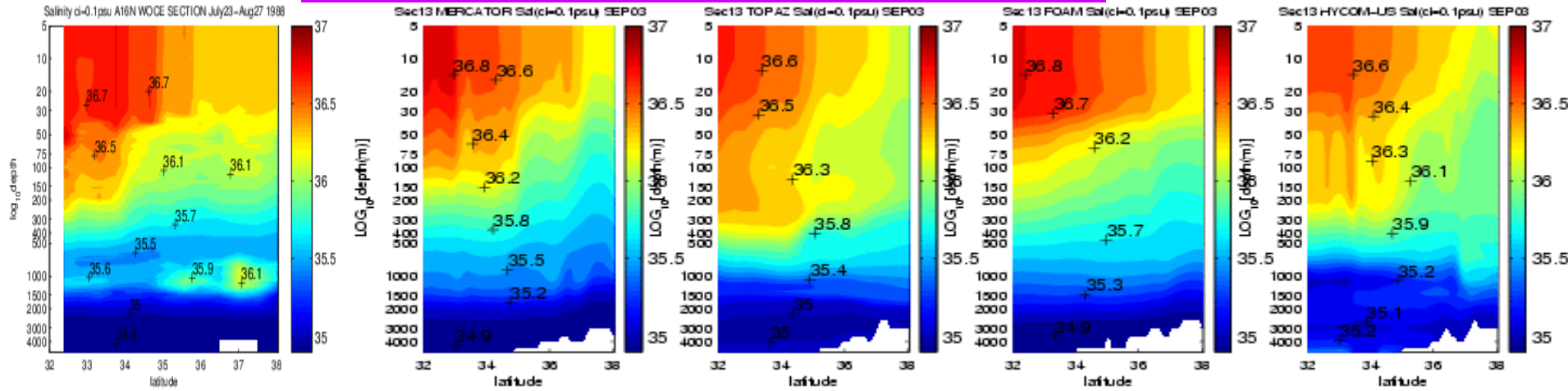
SECTION 26 48°N EKE ( $\text{cm}^2/\text{s}^2$ ) ( $\text{cl}=50 \text{ cm}^2/\text{s}^2$ )



- Impact of vertical coordinates

# Azores Section 20°W Salinity

## MADEIRA MODE WATER, 20W, SALINITY



WOCE A16N JUL AUG 1988

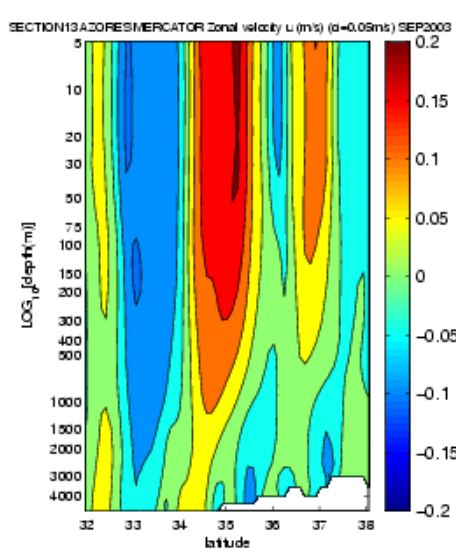
MERCATOR

TOPAZ

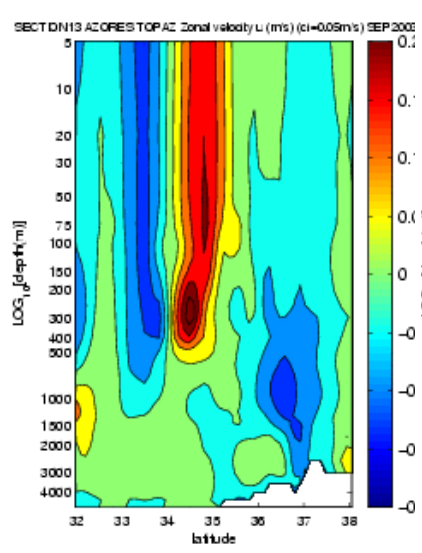
FOAM

HYCOM

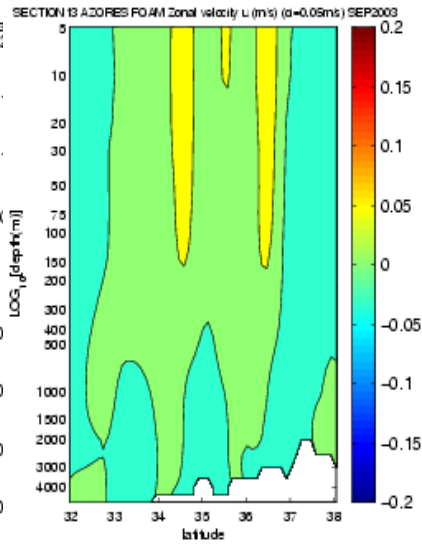
# ZONAL VEL -SECTION 13 - AZORES - SEPT2003



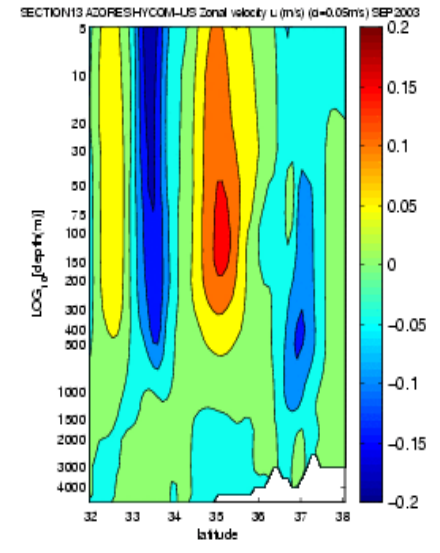
**MERCATOR**



**TOPAZ**



**FOAM**

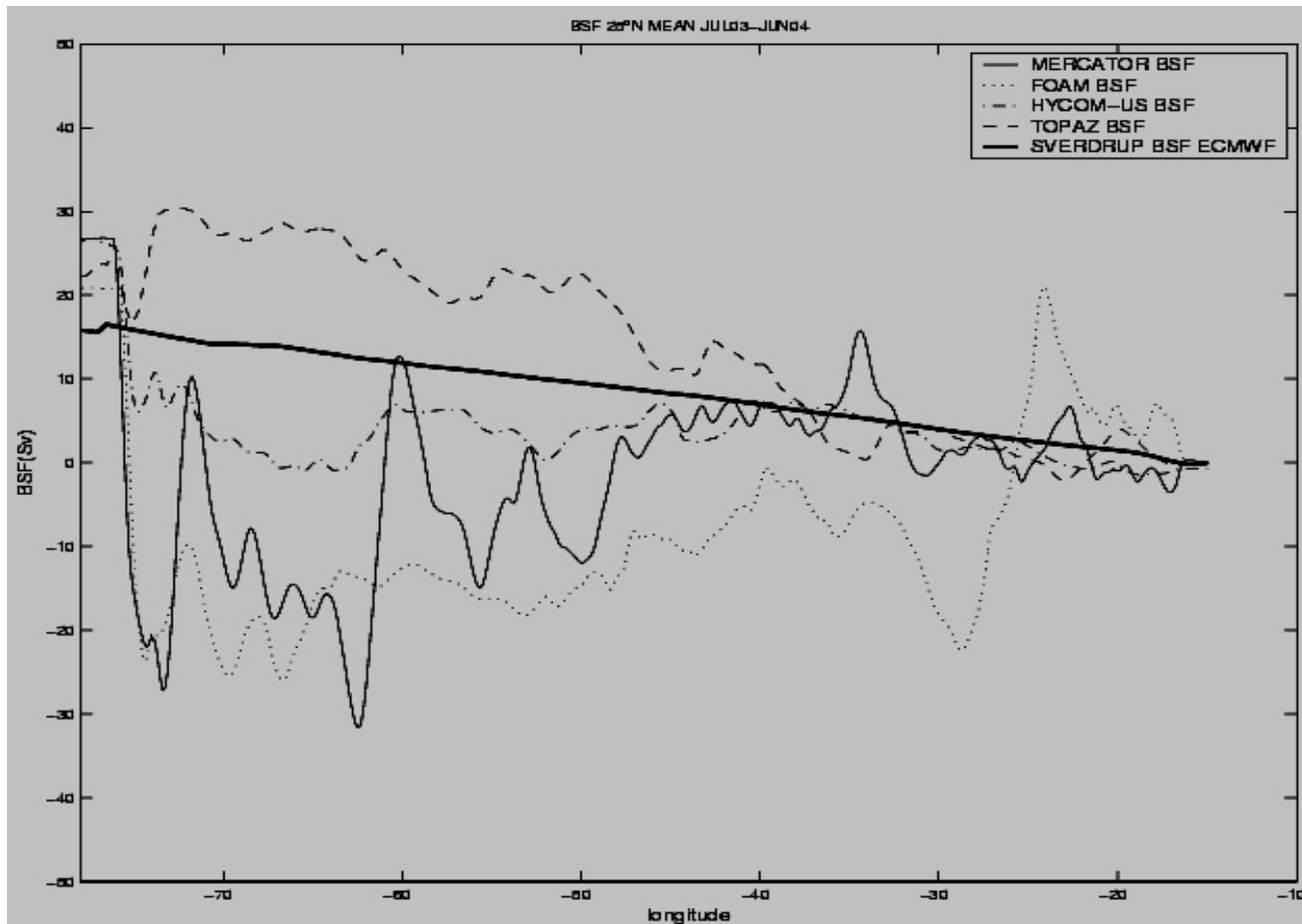


**HYCOM-US**

- Impact from assimilated data  
(SLA and/or ARGO)



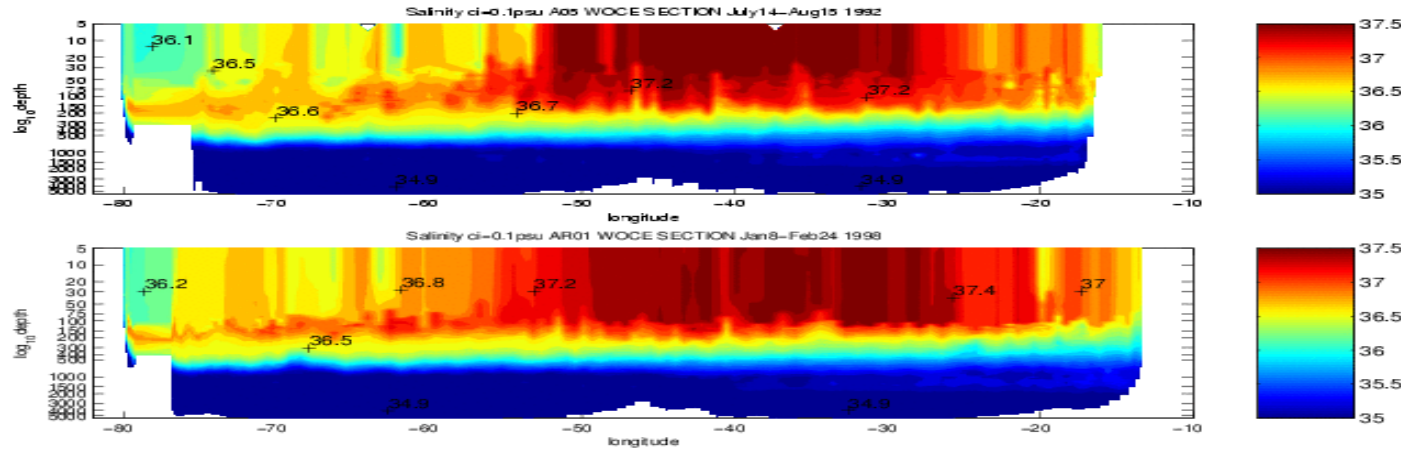
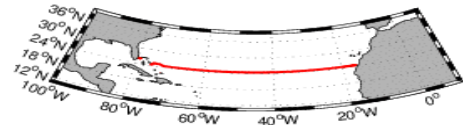
# Barotropic Streamfunction at 25N Sverdrup Streamfunction



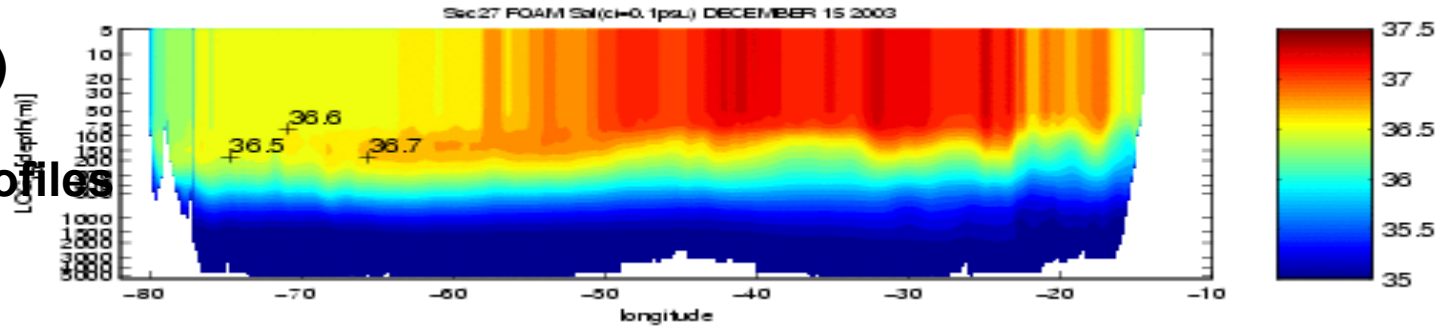
# IMPACT OF ASSIMILATION OF ARGO SALINITY PROFILE

## Class2 Zonal Section 26°N Salinity

WOCE

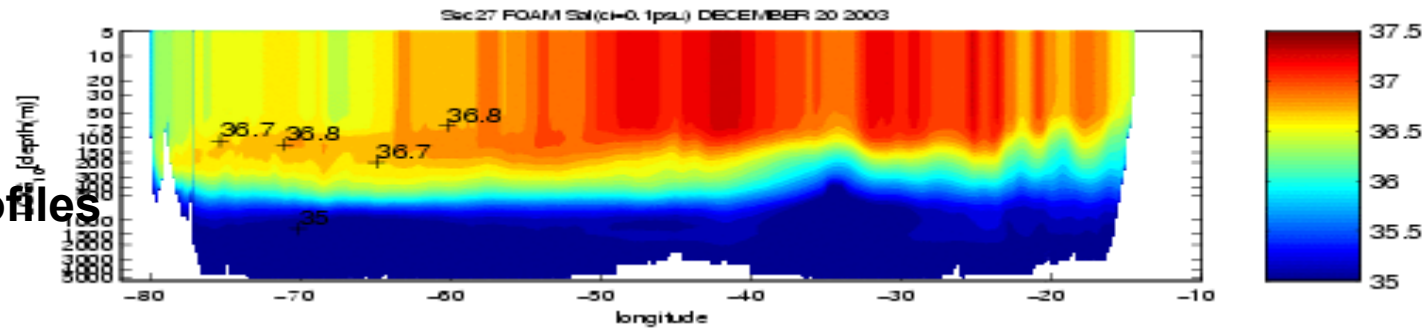


FOAM (DEC15 2003)  
Before assimilation  
of ARGO salinity profiles

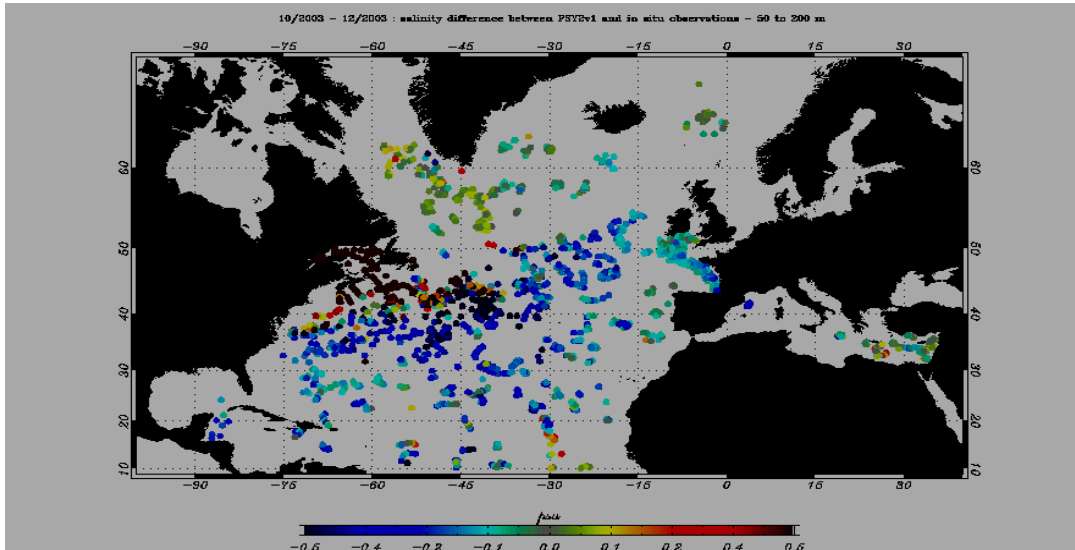


assimilation of ARGO salinity profiles from DEC17 2003 on

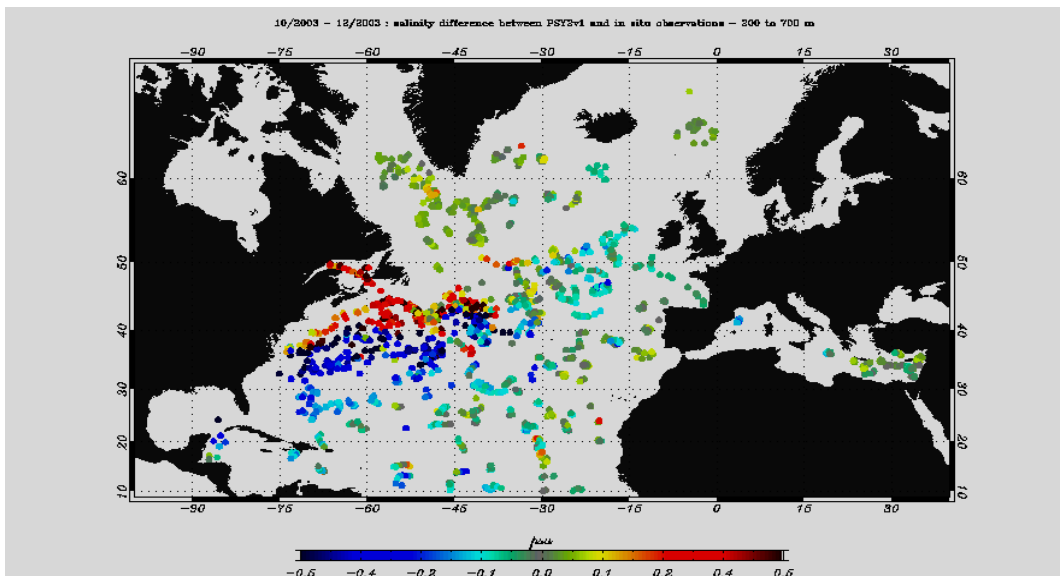
FOAM (DEC20 2003)  
After assimilation  
of ARGO salinity profiles



# In situ Salinity data available from 10-2003 to 12-2003

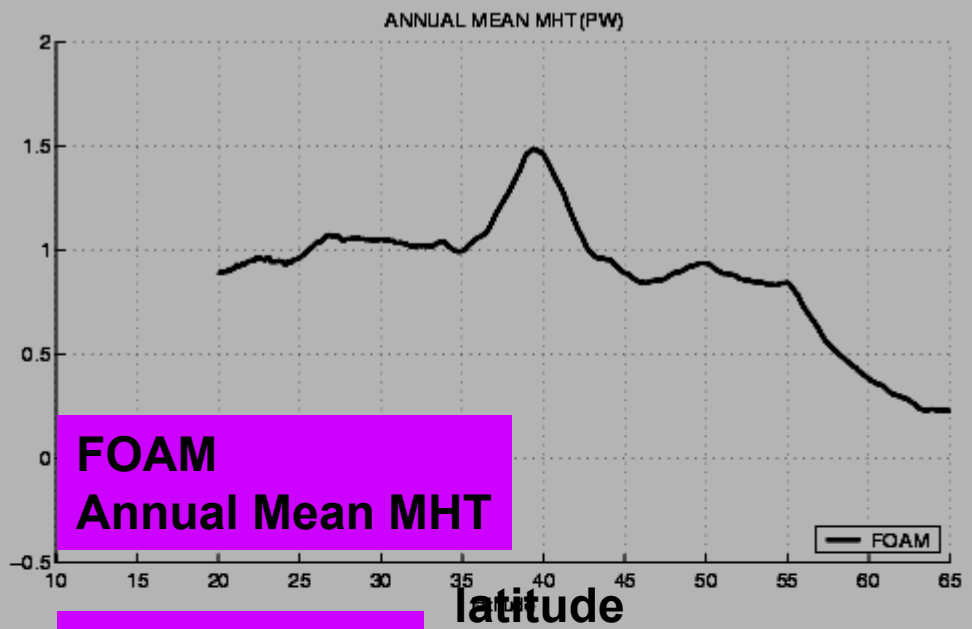
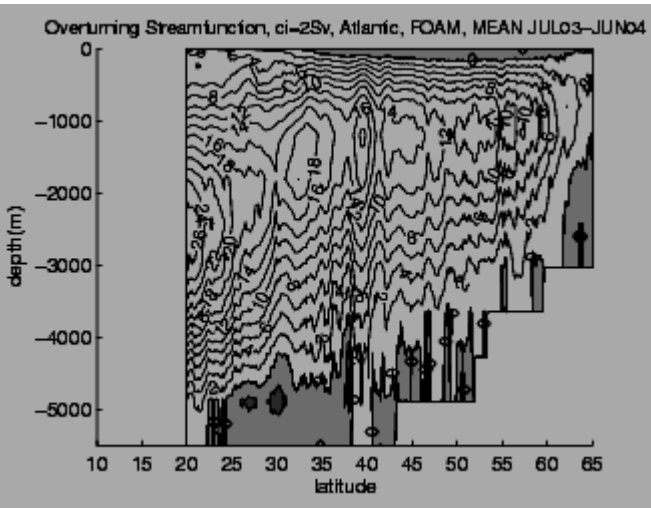


**50-200m**



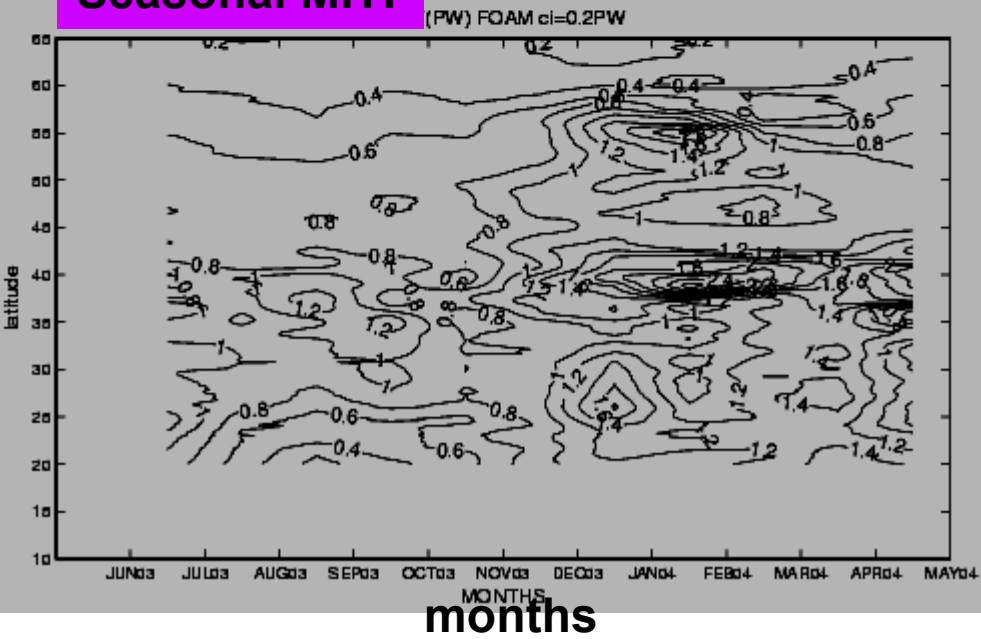
**200-700m**

# FOAM OVERTURNING



# FOAM Annual Mean MHT

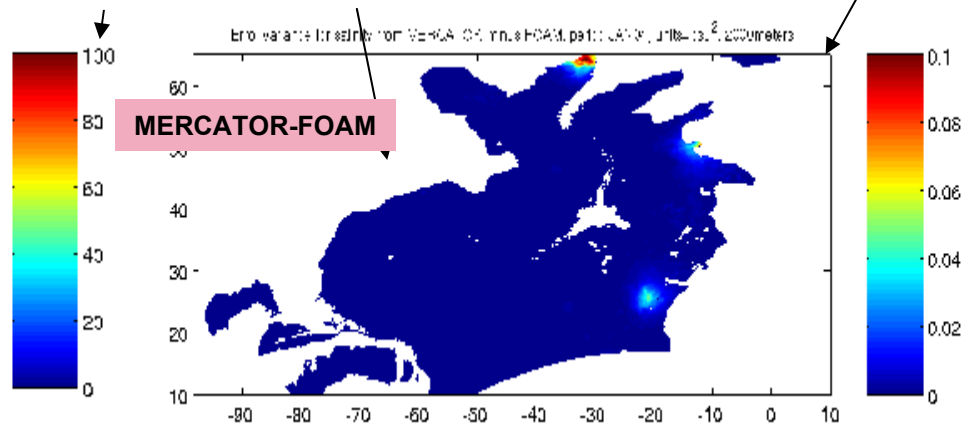
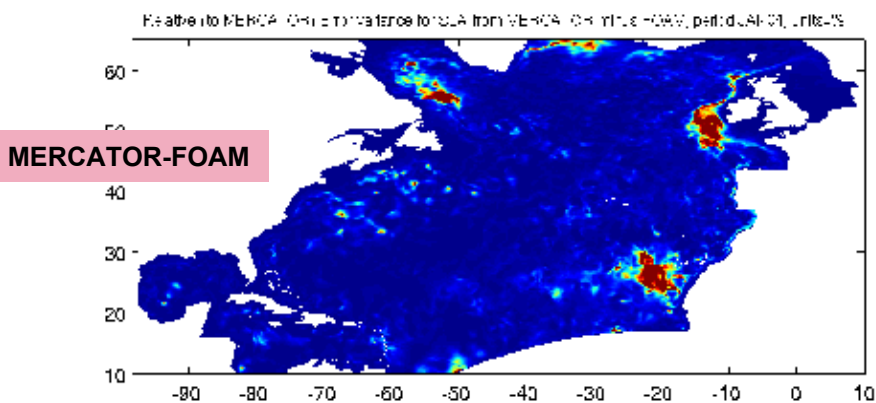
# FOAM Seasonal MHT



# Relative Variance of the Differences for High frequency, JAN04

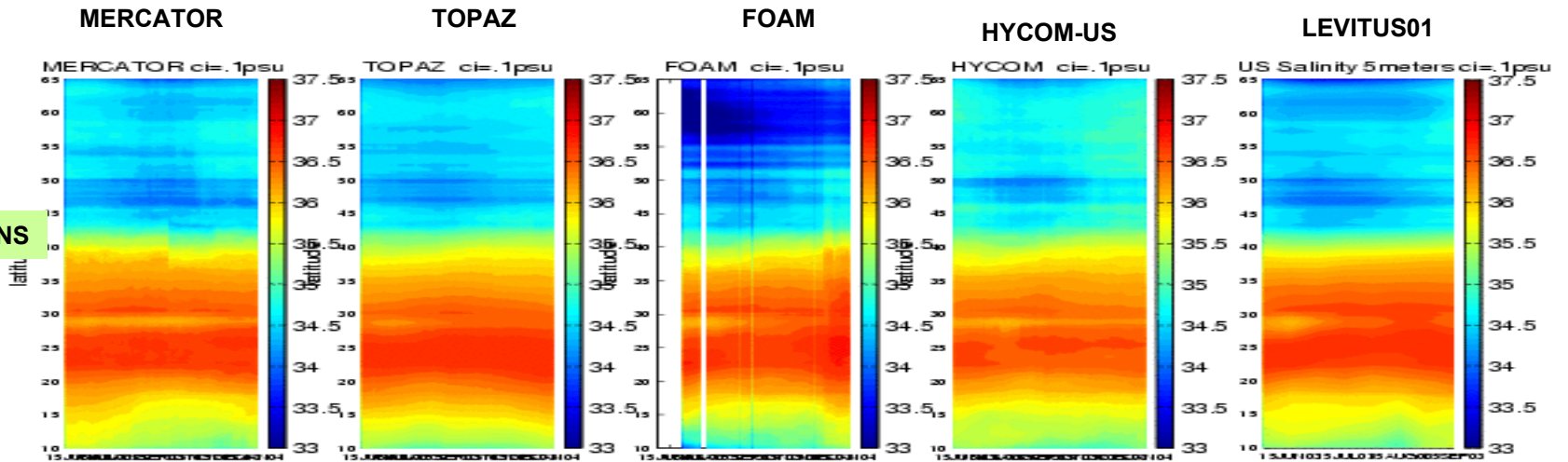
Variance of the  
differences for SLA,  
JAN04,  
units=%

Variance of the  
differences for Salinity,  
JAN04,  
units= $\text{psu}^2$ , 2000meters

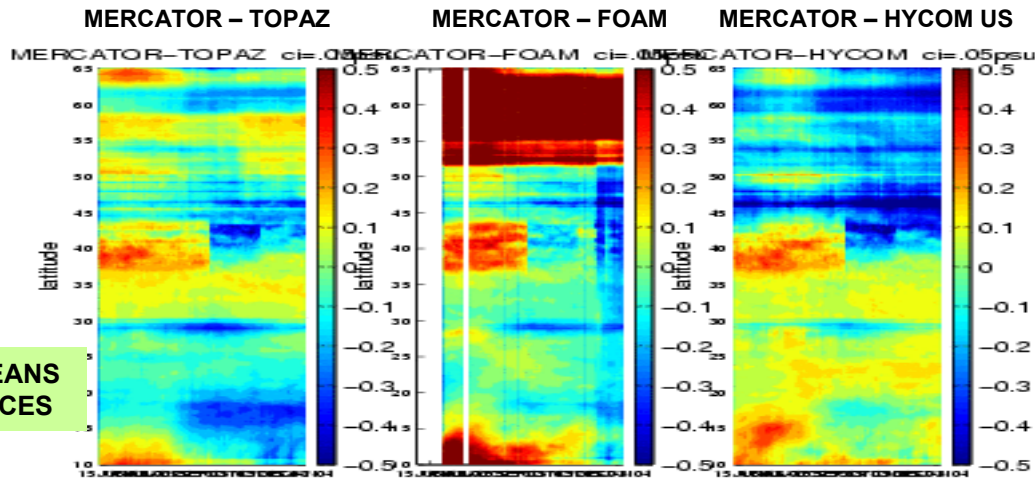


# Hovmuller plots of ZONAL MEAN SURFACE (5meters) Atlantic SALINITY

ZONAL MEANS



ZONAL MEANS DIFFERENCES



- Class3

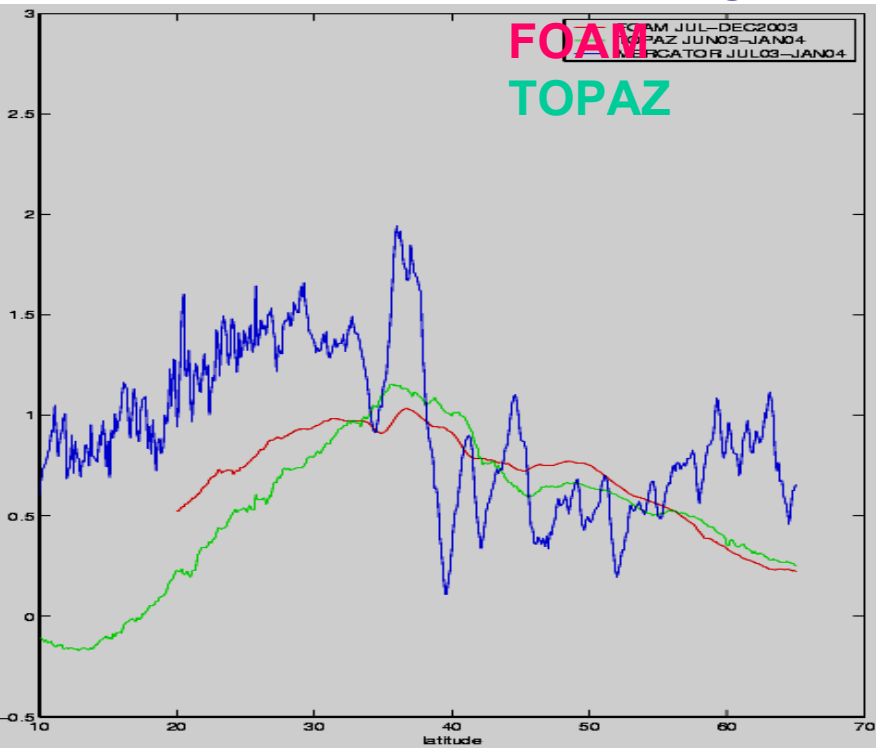
# MERIDIONAL HEAT TRANSPORT

## JUL 1st 03- DEC 1st 03

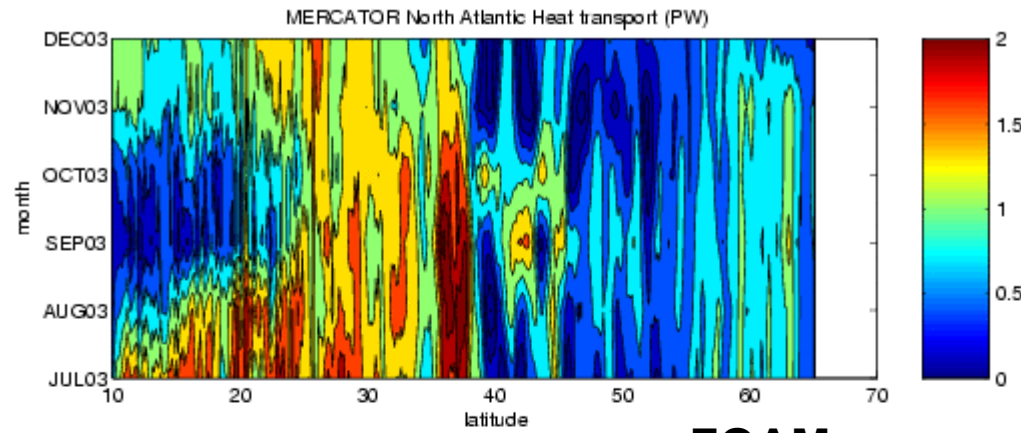
MERCATOR

FOAM

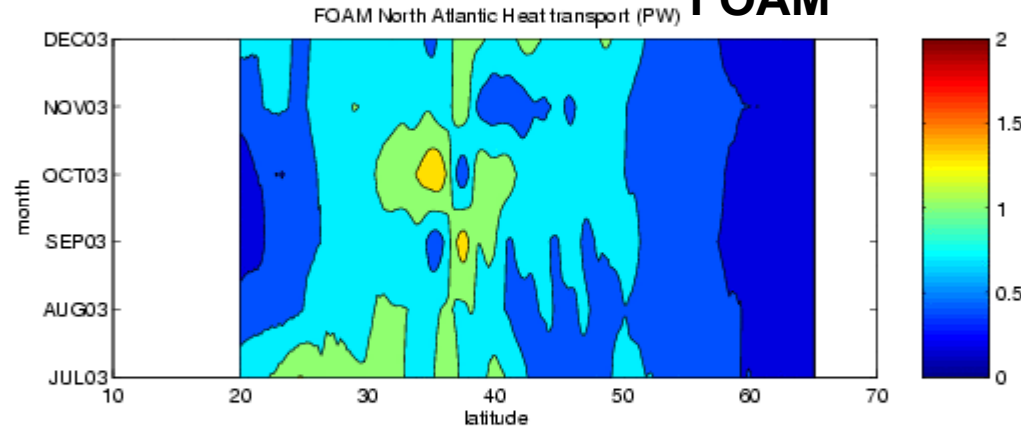
TOPAZ



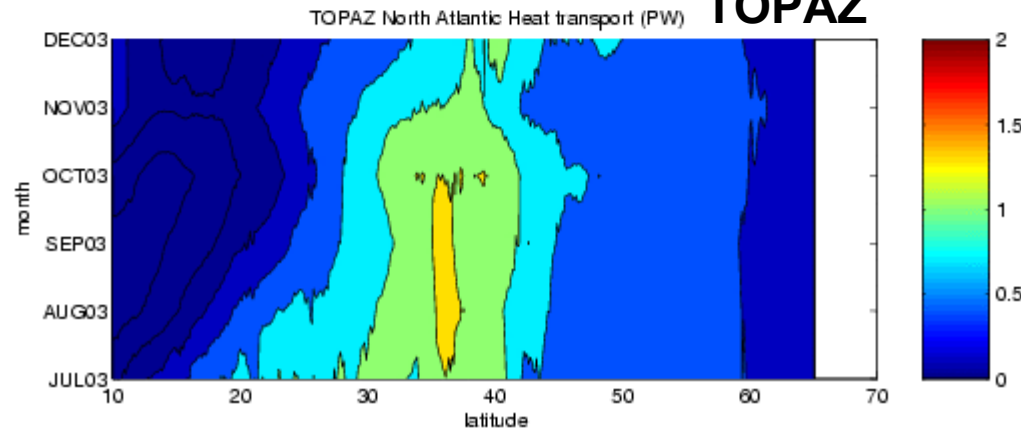
MERCATOR



FOAM



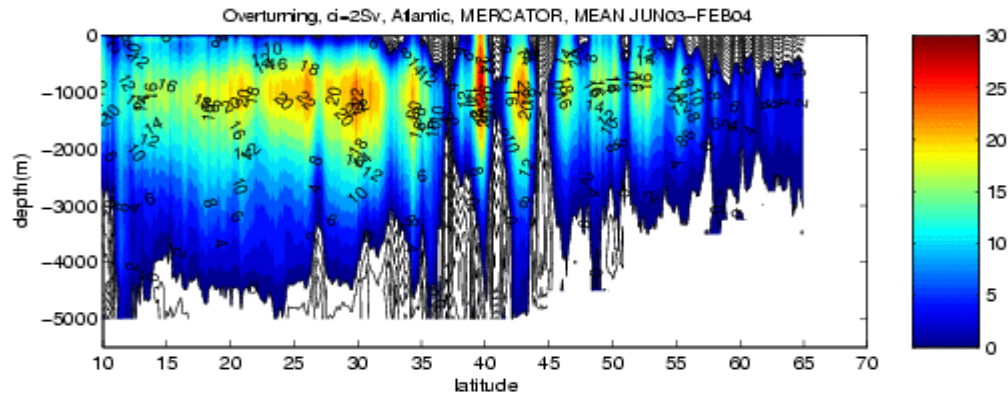
TOPAZ



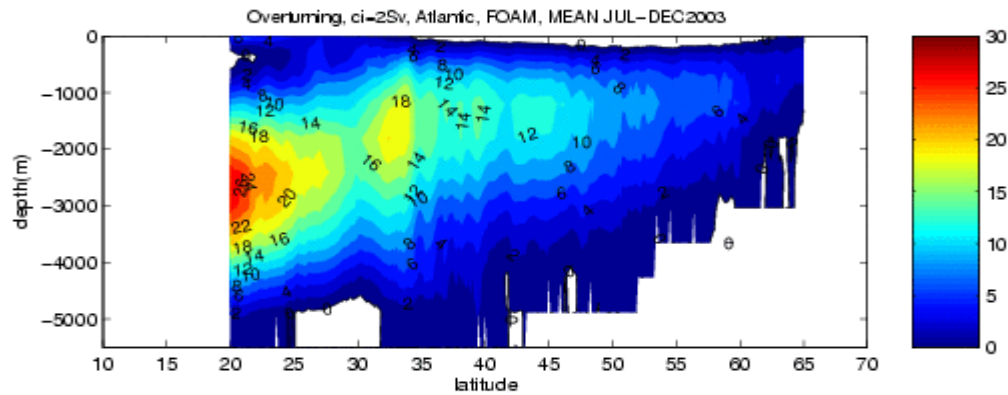


# OVERTURNING STREAM FUNCTION $CI=2Sv$

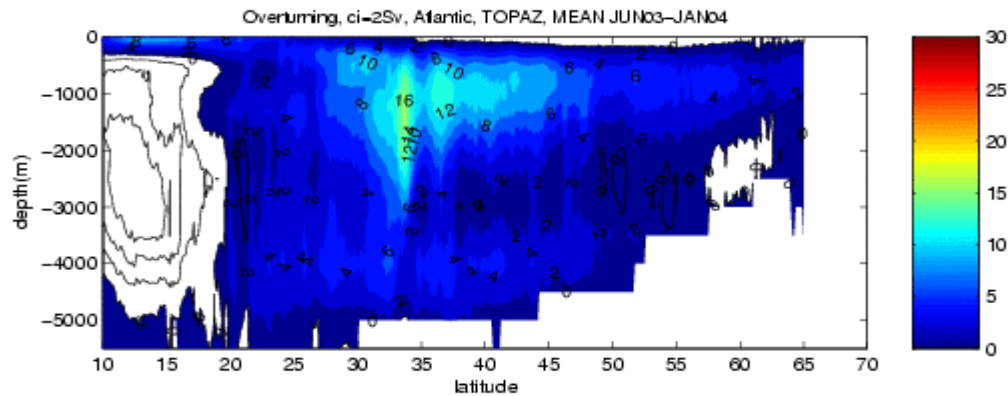
MERCATOR



FOAM



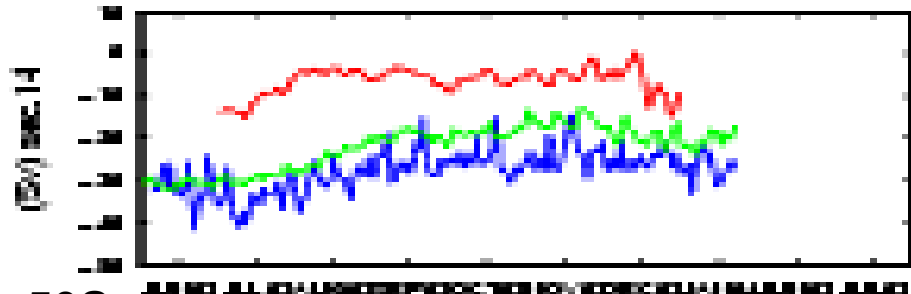
TOPAZ



No AABW=  
No Isobaric effect  
in Hycom  
Sigma\_0 discretization  
(Sun et al. 1999)

MERCATOR  
FOAM  
TOPAZ

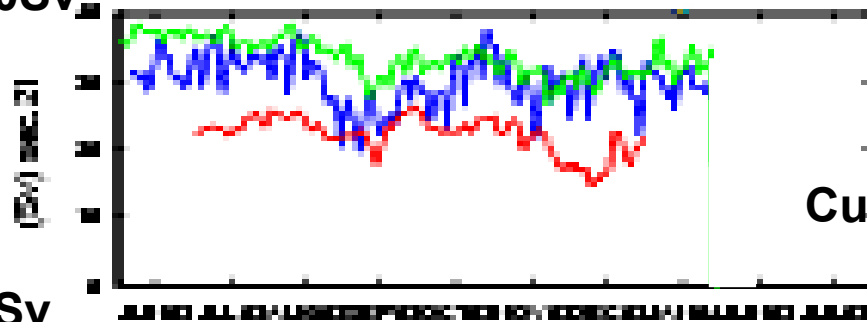
10Sv



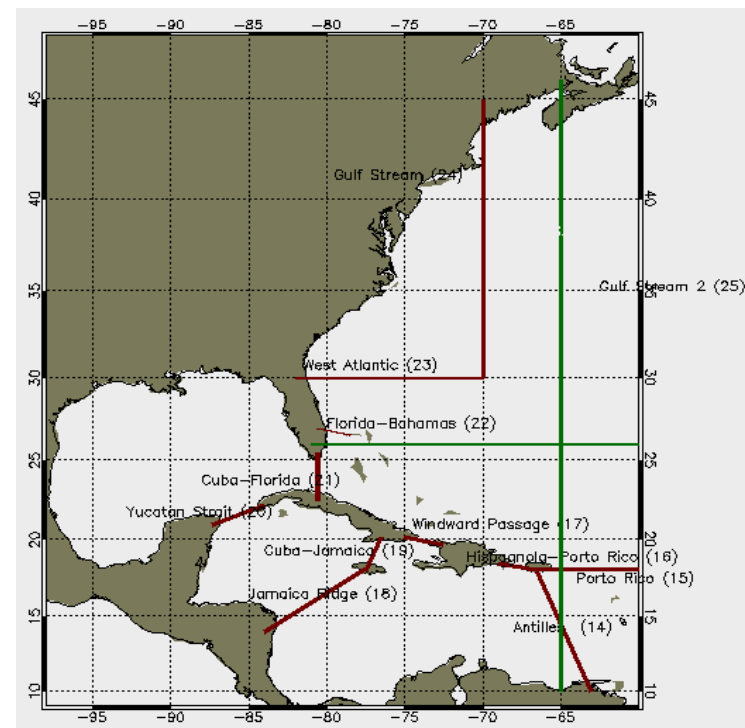
Antilles

-50Sv

40Sv



Cuba Florida



# Constant Upgrade of the systems

## Main events

- **Mercator** Oct1 03 and Nov26 03 : upgrade MSSH  
Vertical diffusivity in Mediterranean basin  
New system with multivariate data assimilation
- **Topaz** June04 : upgrade Hycom version  
Correction on assimilation of SLA  
Inverse barometer effect removed
- **Foam** Dec18 03 : Assimilation of Argo at all depth  
March10 04 : Correction of altimeter Assimilation  
Change of viscosity (Gulf stream path)  
Better quality control for Salinity profiles
- **Mfs** June04 : Use of 20 Eofs (rather than 1)  
Runoff

# Conclusion

MERSEA web site: [www.mersea.eu.org](http://www.mersea.eu.org)

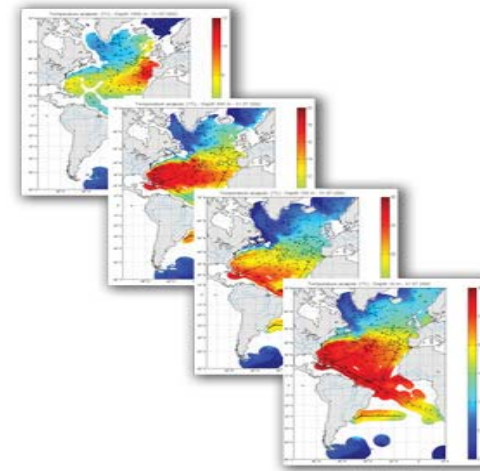
- **1st time such an inter-comparison exercise is conducted on 5 forecasting systems over Atlantic & Mediterranean Basins. Successful prototype. Strength and weakness shown. Soon Global ocean. Methodology adopted by GODAE.**
- Class1-2-3 ready. Working on Class4.
- Common methodology+inter-comparison fosters interactions
- Order ~0 intercomparison but it triggered many changes in the systems
  
- **Watch length of spin up for deep water masses (drift away from Clim if spun up too long).**
- **No clear differences on Mixed Layer Depths between KPP/TKE/Kraus-Turner mixing parameterization.**
- **The higher the horizontal resolution, the more realistic the EKE.**
- **Huge importance of choice of MSSH on system behavior.**
- **Northern overflows: Models with relaxation or Ice model with assimilation of ice concentration are too warm. Check the Arctic behavior during Mersea-IP.**
- **Med Water Overflows : Relaxation or entrainment parameterization to MOW not well done.**
- **Multivariate data assimilation improve the systems (but watch data quality control !)** .
- **Mersea-strand1 is over. More work to be done during MERSEA-IP:**
  - Class4 diagnostics results**
  - Comparison with IN SITU DATA : Coriolis/Armor/ADCP/XBT data sets.**
  - Need for definition of synthetic indicators.**
  - Look at Arctic region**
  - Definition of Metrics for GODAE basins/Arctic ocean...**

# CORIOLIS OBJECTIVE ANALYSIS For the Atlantic Ocean

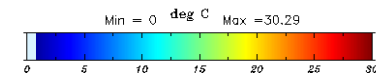
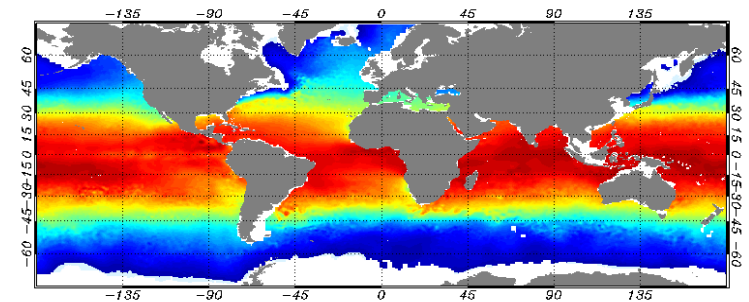
T/S Coriolis profiles

## ARMOR ANALYSIS For the Global Ocean

MSLA Salto/Duacs+ T/S Coriolis profiles  
+ SST Reynolds + Coriolis drifters



ARMOR analysed temperature : T on 03-03-2004 near 0m



10-20% ice cover  
jul day 19785



ADCP, XBT(Meds), SEA LEVEL GAUGE in MED, .....



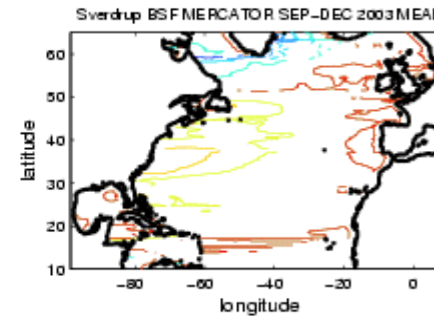
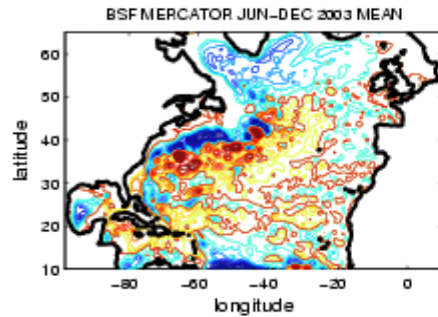
# The class 4 metrics in the observational space

RMSINNOV	$\frac{1}{N-1} \sqrt{\sum (o - Hh)^2}$	$\frac{\sum (o - Hc)(Hh - Hc)}{\sqrt{\sum (o - Hc)^2} \sqrt{\sum (Hh - Hc)^2}}$
RMSCLIM	$\frac{1}{N-1} \sqrt{\sum (o - Hc)^2}$	Undefined
RMSINNOV1	$\frac{1}{N-1} \sqrt{\sum (o - Hf)^2}$	$\frac{\sum (o - Hc)(Hf - Hc)}{\sqrt{\sum (o - Hc)^2} \sqrt{\sum (Hf - Hc)^2}}$
RMSRESID	$\frac{1}{N-1} \sqrt{\sum (o - Ha)^2}$	$\frac{\sum (o - Hc)(Ha - Hc)}{\sqrt{\sum (o - Hc)^2} \sqrt{\sum (Ha - Hc)^2}}$
RMSPERS	$\frac{1}{N-1} \sqrt{\sum (o - Hp)^2}$	$\frac{\sum (o - Hc)(Hp - Hc)}{\sqrt{\sum (o - Hc)^2} \sqrt{\sum (Hp - Hc)^2}}$

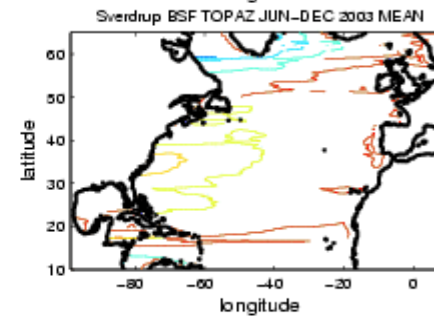
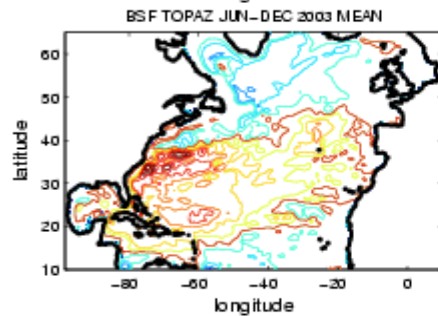
# JUNE\_DEC2003 Mean Barotropic Stream Function (ci=10Sv)

## And Sverdrup Barotropic Stream Function (ci=10Sv)

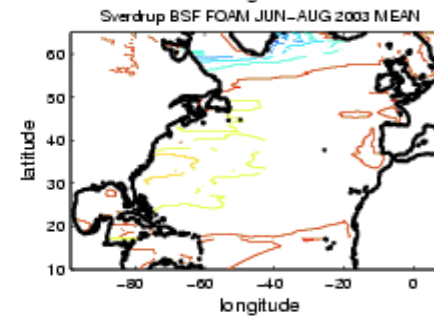
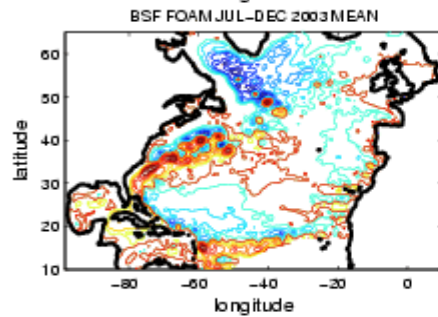
MERCATOR



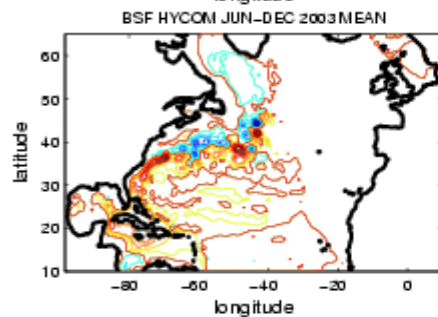
TOPAZ



FOAM



HYCOM-US





# Relative (to Mercator) Variance of the Differences for High frequency SLA, JAN04, units=%

